

ECE609 Spring06  
**HOMWORK 5 - SOLUTIONS**  
 Two-Terminal Devices

**1 P-N junctions (25pts)**

1. •

$$qV_i = E_g + k_B T \ln \left( \frac{N_A N_D}{N_C N_V} \right) = 1.14 eV$$

- $W = 1 \mu m$
- $E = 1.14 / 10^{-4} = 11400 V/cm$

2. • The thermal equilibrium densities are: -In the p-type region:  $p = N_a = 2 * 10^{16} cm^{-3}$  and  $n = n_i^2 / p = 10^{20} / 2 * 10^{16} = 5 * 10^3 cm^{-3}$ .  
 -In the n-type region:  $n = N_d - N_a = 9 * 10^{16} cm^{-3}$  and  $p = n_i^2 / n = 10^{20} / (9 * 10^{16}) = 1.11 * 10^3 cm^{-3}$ .

- The built-in potential is obtained from:

$$V_i = k_B T / q \ln \left( \frac{n_n p_p}{n_i^2} \right) = 0.79 V$$

- $V_i = 0.63 V$

3.  $V_i = 0.76 V$

$$W = 2(\epsilon(N_a + N_d)(V_i - V_a)/(qN_a N_d))^{1/2}$$

since  $W = l_n + l_p$ , and  $l_n N_d = l_p N_a$  it comes:  $l_n = W N_a / (N_a + N_d)$ .

	$V_a = 0V$	$V_a = 0.5V$	$V_a = -2.5V$
$x_d$	$0.315 \mu m$	$0.143 \mu m$	$0.703 \mu m$
$E$	$40 kV/cm$	$18 kV/cm$	$89 kV/cm$
$V_n$	$0.105 V$	$0.0216 V$	$0.522 V$

4.  $V_i = 0.83 V$  so at zero bias  $W = 0.33 \mu m$ , and then  $C = 3.17 pF$ .

5.

$$I = qA \left( \frac{D_n n_{p0}}{L_n} + \frac{D_p p_{n0}}{w_n} \right) * (\exp(q\beta V_a) - 1)$$

- $D_n = 1000 * 0.0258 = 25.8 cm^2/Vs$
- $D_p = 300 * 0.0258 = 7.75 cm^2/Vs$
- $n^{p0} = n_i^2 / N_a = 10^{20} / 10^{16} = 10^4 cm^{-3}$
- $p_{n0} = n_i^2 / N_d = 10^{20} / 4 * 10^{16} = 2.5 * 10^3 cm^{-3}$
- $L_n = 161 \mu m$
- $I = 40.7 mA$

## 2 Metal-Semiconductor Junctions (15pts)

1.  $V_B = V_M - \Xi = 0.45V$ , we know that the built-in potential is given by:

$$V_i = V_B - (k_B T/q) \ln(N_c/N_d) = 0.30V.$$

For the p-type structure:

$$V_B = \xi + E_g/q - V_M = 0.67V$$

and

$$V_i = V_B - (k_B T/q) \ln(N_v/N_a) = 0.53V.$$

2. The depletion layer width equals:  $W = 0.26\mu m$ ,  $E = 4.0 * 10^5 V/cm$ ,  $V = 5.3V$ ,  $C = 40nF/cm^2$ .