

# HOMWORK 6 - PRACTICE FINAL EXAM

## MOS capacitors and MOSFET

### 1 MOS capacitors

1. Calculate the flatband voltage of a silicon nMOS capacitor with a substrate doping  $N_a = 10^{17} \text{cm}^{-3}$  and an aluminum gate (with a “work function”  $V_M = 4.1V$ ). Assume (i) there is no fixed charge in the oxide or at the oxide-silicon interface, (ii) we are at room temperature, (iii)  $n_i = 10^{10} \text{cm}^{-3}$   
 $V_{FB} = -0.93V$
2. Using the result previously obtained, calculate the threshold voltage of a silicon nMOS capacitor with a substrate doping  $N_a = 10^{17} \text{cm}^{-3}$ , a  $20\text{nm}$  thick oxide ( $\epsilon_{ox} = 3.9\epsilon_0$ ) and an aluminum gate ( $V_M = 4.1V$ ). Assume there is no fixed charge in the oxide or at the oxide-silicon interface.  
 since  $V_F = 0.42V$ ,  $V_T = -0.09V$

### 2 MOSFET

1. Calculate the drain current of a silicon nMOSFET with  $V_T = 1V$ ,  $W = 10\mu\text{m}$ ,  $L = 1\mu\text{m}$  and  $t_{ox} = 20\text{nm}$ . The device is biased with  $V_{GS} = 3V$  and  $V_{DS} = 5V$ . Use the quadratic model, a surface mobility of  $300\text{cm}^2/V\text{s}$  and set  $\epsilon_{Si} = 3.9$ . Also calculate the transconductance at  $V_{GS} = 3V$  and  $V_{DS} = 5V$  and the output conductance at  $V_{GS} = 3V$  and  $V_{DS} = 0V$ .  
 The MOSFET is biased in saturation since  $V_{DS} > V_{GS} - V_T$   
 so  $I_D = 1.04\text{mA}$   
 and  $g_m = 1.04\text{mS}$ ,  $g_d = 1.04\text{mS}$ ,  $S$  for Siemens
2. Repeat the question above using the variable depletion layer model. Use  $V_{FB} = -0.807V$  and  $N_a = 10^{17} \text{cm}^{-3}$ . For the transconductance, you will derive the value of the modified mobility  $\mu_n^*$  and you will comment on the result of the conductance.  
 To find out whether the MOSFET is biased in saturation, we need first to calculate  $V_{Dsat} = 1.39V$   
 We then get  $I_D = 0.7\text{mA}$   
 $g_m = 0.52\text{mS}$  with  $\mu_n^* = 149\text{cm}^2/V\text{s}$   
 $g_d = 1.04\text{mS}$ . which is the same as that of example above since the depletion layer width is constant for  $V_{DS} = 0$ .