

4.1 Hydrodynamic volume force in polar coordinates

Derive the components of the hydrodynamic volume force, Σ , in cylindrical polar coordinates.

4.2 Hydrodynamic pressure

Demonstrate that the negative of the pressure, $-p \equiv \frac{1}{3}\text{trace}(\boldsymbol{\sigma})$, is the average of the normal component of the traction exerted on the surface of a spherical fluid parcel with infinitesimal dimensions.

4.3 Energy dissipation in shear flow

Compute the rate of energy dissipation inside a parcel of a Newtonian fluid in simple shear flow with velocity $u_x = \xi y$, $u_y = 0$, $u_z = 0$, where ξ is a constant shear rate.

4.4 Function of a tensor

Consider a function $f(x)$ defined through its Taylor series expansion. Show that if \mathbf{T} is a tensor, then $f(\mathbf{T})$ is also a tensor.