

Steps for Flawless Control Volume Analysis

(1) Draw a picture of the problem.

- (a) Include everything you know in the picture.
- (b) Include a coordinate system (and stick to it).
- (c) Label all the important exits/entrances (with numbers usually).
- (d) Draw the normal vectors at exits/entrances (and where pressure acts).

(2) Draw the control volume (dotted line).

This is the art, and often the key, to successful control volume analysis.

- (a) Place boundaries where you know something.
- (b) Place boundaries where you want to know something.
- (c) Consider the orientation of boundaries (perpendicular is often very wise).
- (d) If the boundary follows a wall, make sure that you indicate whether it includes the wall.

(3) Understand the physics.

- (a) Indicate all significant forces on the sketch (and their direction).
- (b) Indicate all significant energy sources (and where the energy goes).
- (c) Account for all the fluids or solids which cross the control volume boundaries.

(4) Define the model.

Control Volume Analysis is always approximate - *so list your simplifying assumptions.*

steady-state
uniform flow
frictionless (ignore viscosity)
incompressible / perfect gas
gravity is unimportant
isothermal (no temperature change)
etc...

(5) Apply fundamental principals. (Conservation of Mass, Momentum, Energy)

- (a) Write down the equations that apply. (see above)
- (b) Simplify the equations given the assumptions
(this is where 70% of your mistakes will be - be careful – go slowly)

(6) Solve the equations.

- (a) Check that: the # of equations = the # of unknowns.
- (b) If not - may need additional equations (e.g. equation of state, extra CV).
- (c) Solve the equations.
- (d) Check the Units.
- (e) Check obvious limiting cases. *(Does the answer make sense?)*