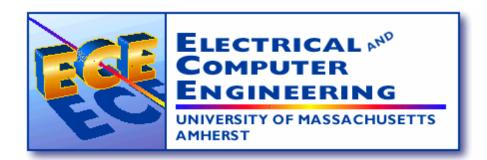
# **ENGIN 112**

## **Intro to Electrical and Computer Engineering**

#### Lecture 21 Analyzing Sequential Circuits



#### **Overview**

#### ° Understanding flip flop state:

• Stored values inside flip flops

### ° Clocked sequential circuits:

• Contain flip flops

#### ° Representations of state:

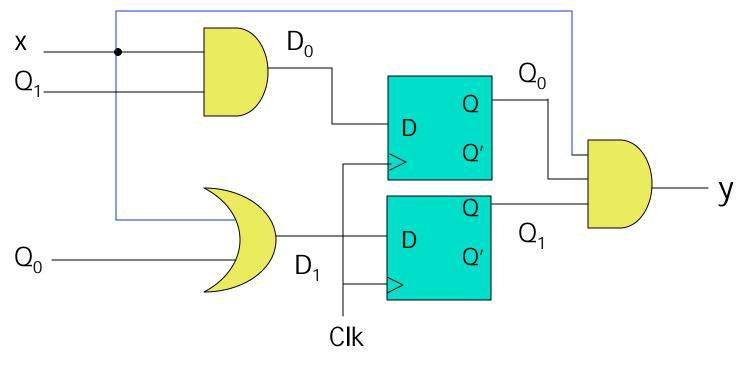
- State equations
- State table
- State diagram

#### ° Finite state machines

- Mealy machine
- Moore machine

#### Flip Flop State

 Behavior of clocked sequential circuit can be determined from inputs, outputs and FF state



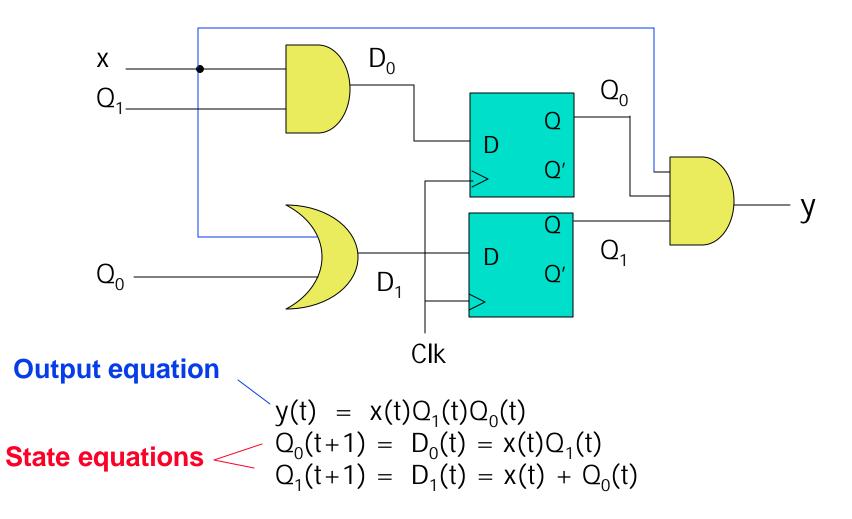
$$y(t) = x(t)Q_1(t)Q_0(t)$$
  

$$Q_0(t+1) = D_0(t) = x(t)Q_1(t)$$
  

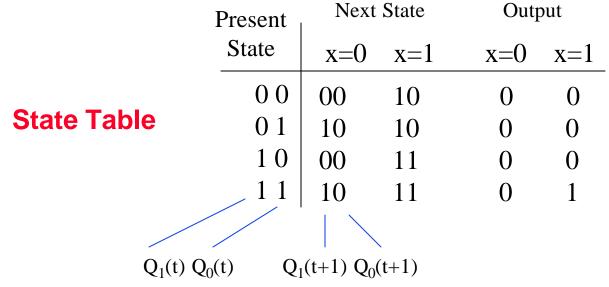
$$Q_1(t+1) = D_1(t) = x(t) + Q_0(t)$$

#### **Output and State Equations**

<sup>o</sup> Next state dependent on previous state.



- Sequence of outputs, inputs, and flip flop states enumerated in state table
- **Present state** indicates current value of flip flops
- Next state indicates state after next rising clock edge
- Output is output value on current clock edge



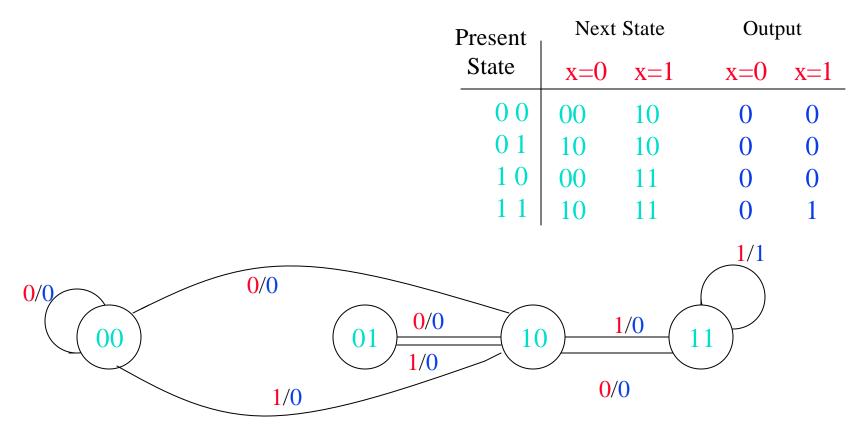
ENGIN112 L21: Analyzing Sequential Circuits

- All possible input combinations enumerated
- All possible state combinations enumerated
- Separate columns for each output value.
- Sometimes easier to designate a symbol for each state.

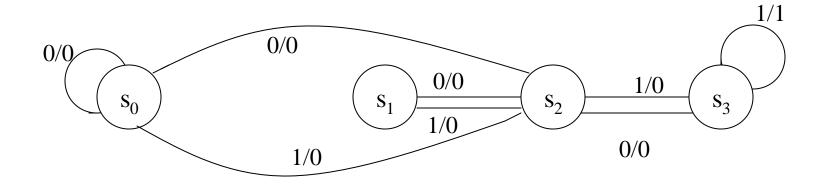
	Present	Next State		Output	
Let:	State	x=0	x=1	x=0	x=1
$s_0 = 00$	s <sub>0</sub>	s <sub>0</sub>	s <sub>2</sub>	0	0
$s_1 = 01$	s <sub>1</sub>	s <sub>2</sub>	s <sub>2</sub>	0	0
$s_2 = 10$	s <sub>2</sub>	s <sub>0</sub>	S <sub>3</sub>	0	0
$s_3 = 11$	s <sub>3</sub>	s <sub>2</sub>	s <sub>3</sub>	0	1

#### **State Diagram**

- ° Circles indicate current state
- Arrows point to next state
- ° For x/y, x is input and y is output

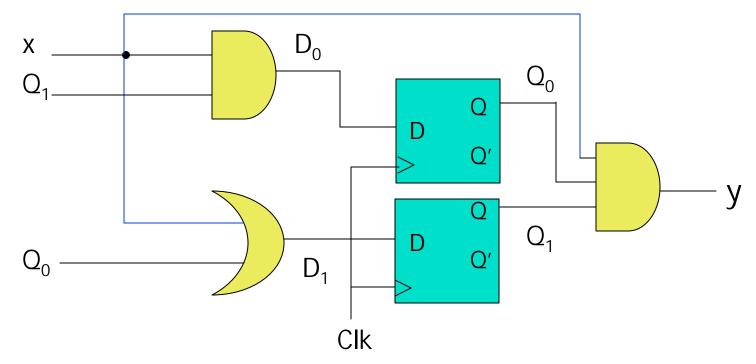


- Each state has two arrows leaving
  - ° One for x = 0 and one for x = 1
- Unlimited arrows can enter a state
- Note use of state names in this example
  - Easier to identify



#### **Flip Flop Input Equations**

 Boolean expressions which indicate the input to the flip flops.



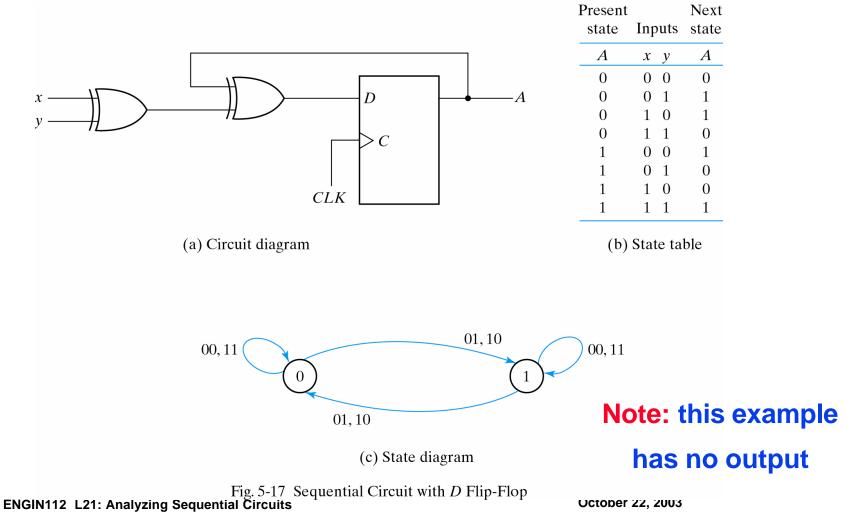
 $D_{Q0} = xQ_1$  $D_{Q1} = x + Q_0$ 



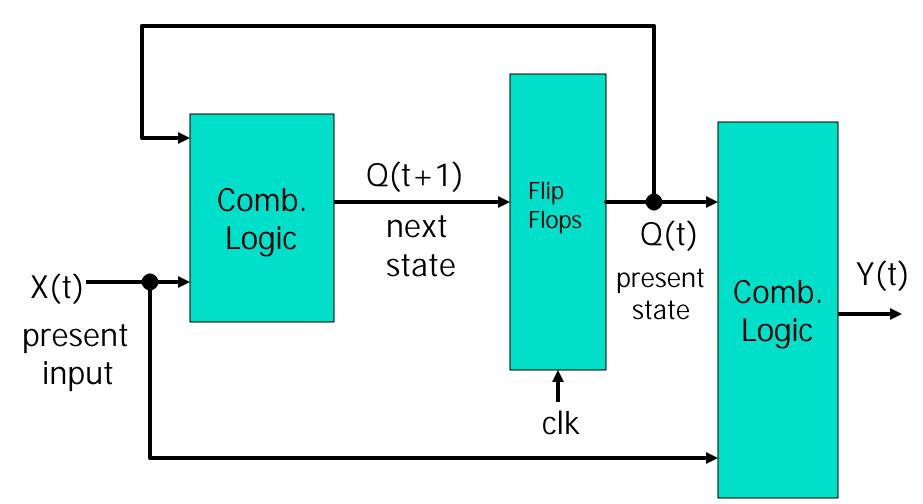
### **Analysis with D Flip-Flops**

Identify flip flop input equations

#### Identify output equation

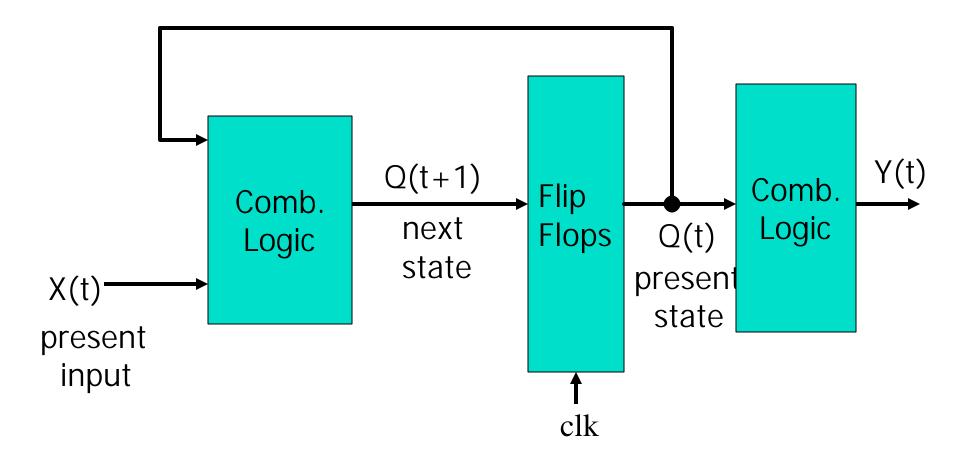


• Output based on state and present input



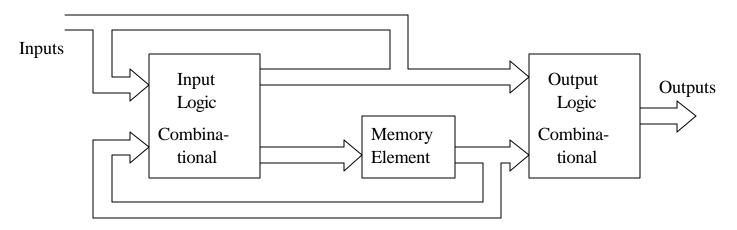
#### **Moore Machine**

Output based on state only

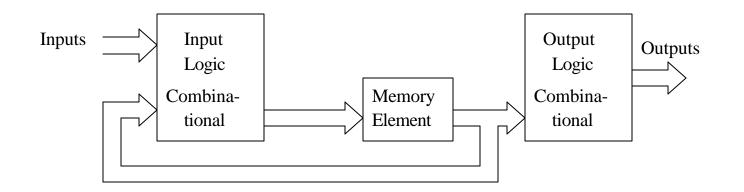


#### Mealy versus Moore

#### Mealy Model

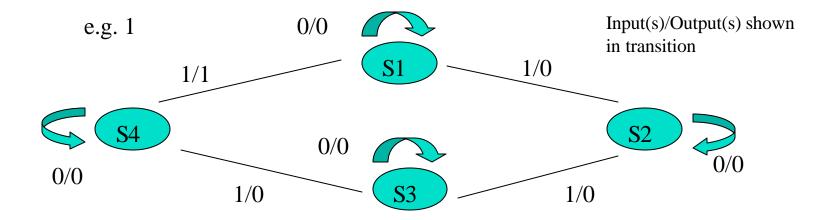


Moore Model



#### State Diagram with One Input & One Mealy Output

- Mano text focuses on Mealy machines
- State transitions are shown as a function of inputs and current outputs.



#### State Diagram with One Input & a *Moore* Output

- Moore machine: outputs only depend on the current state
- Outputs cannot change during a clock pulse if the input variables change
- Moore Machines usually have more states.
- No direct path from inputs to outputs
- Can be more reliable

#### **Clocked Synchronous State-machine Analysis – next class**

#### Given the circuit diagram of a state machine:

- 1 Analyze the combinational logic to determine flip-flop input (excitation) equations:  $D_i = F_i$  (Q, inputs)
  - The input to each flip-flop is based upon current state and circuit inputs.
- 2 Substitute excitation equations into flip-flop characteristic equations, giving transition equations:  $Q_i(t+1) = H_i(D_i)$
- 3 From the circuit, find output equations: Z = G (Q, inputs)
  - The outputs are based upon the current state and possibly the inputs.
- 4 Construct a state transition/output table from the transition and output equations:
  - Similar to truth table.
  - Present state on the left side.
  - Outputs and next state for each input value on the right side.
  - Provide meaningful names for the states in state table, if possible.

# 5 Draw the state diagram which is the graphical representation of state table.

#### Summary

- ° Flip flops contain state information
- <sup>°</sup> State can be represented in several forms:
  - State equations
  - State table
  - State diagram

#### ° Possible to convert between these forms

- ° Circuits with state can take on a finite set of values
  - Finite state machine

#### ° Two types of "machines"

- Mealy machine
- Moore machine