

CEE 680: Water Chemistry

Lecture #34

Precipitation and Dissolution: Basics and
metal solubility

(Stumm & Morgan, Chapt.7)

Benjamin; Chapter 8.7-8.15

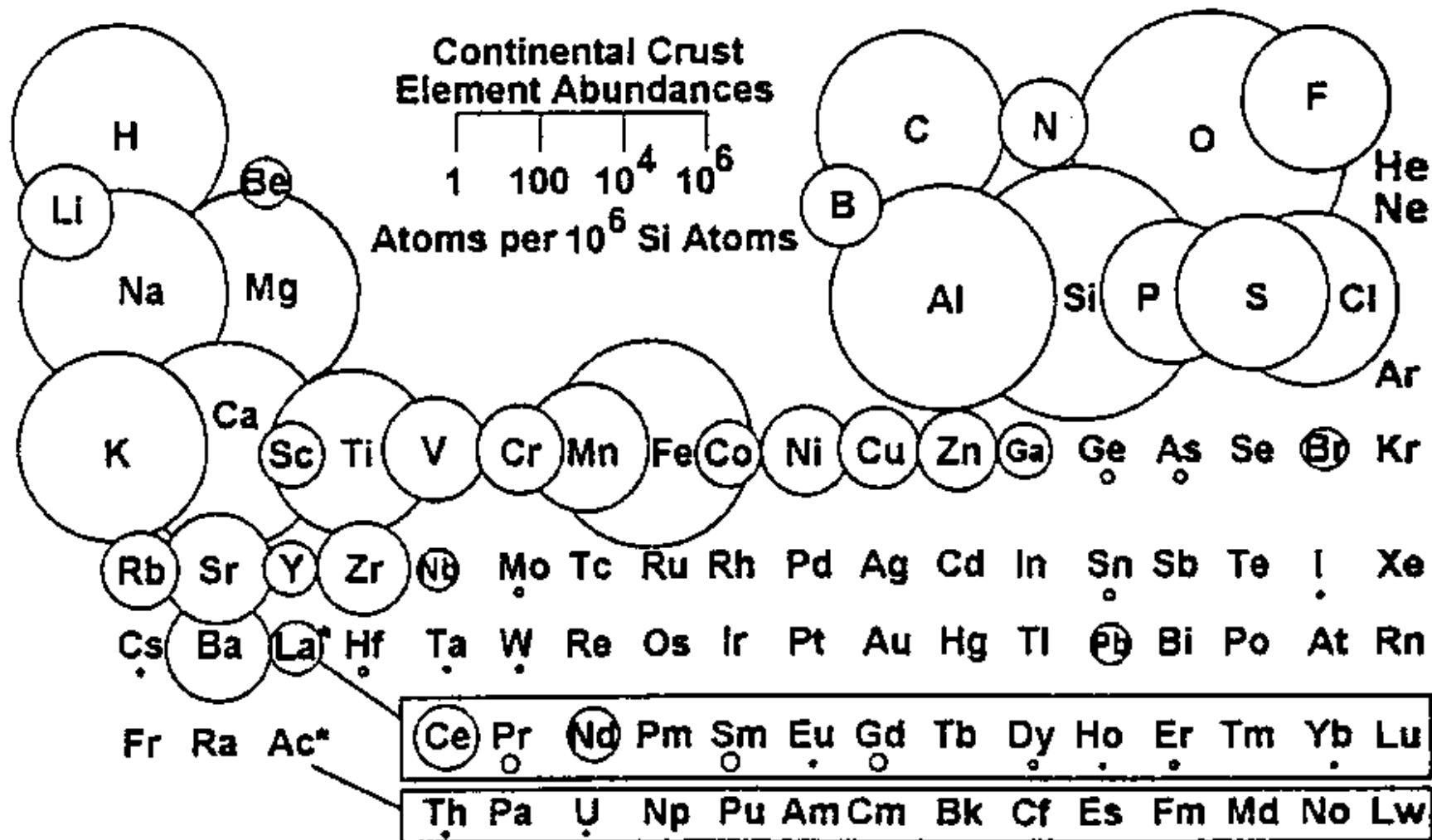
Topics

- Hydrolysis
 - Aquo metal ion gives rise to hydroxo complexes
- Magnesium and Iron Hydroxide solubility

Precipitation and Dissolution

- Environmental Significance
 - Engineered systems
 - coagulation, softening, removal of heavy metals
 - Natural systems
 - composition of natural waters
 - formation and composition of aquatic sediments
 - global cycling of elements
- Composition of natural waters
 - S&M, 3rd ed., figure 15.1 (pg. 873)
 - Benjamin, 2nd ed., figure 1.1

Elemental Abundance in Crust



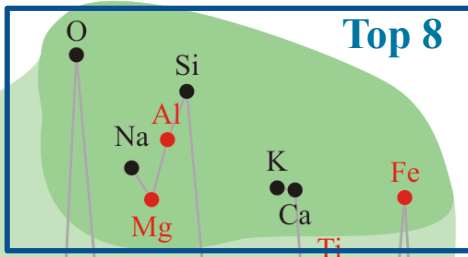
ABUNDANCE OF ELEMENTS IN EARTH'S CRUST

major industrial metals (global production $>3 \times 10^7$ kg/year)

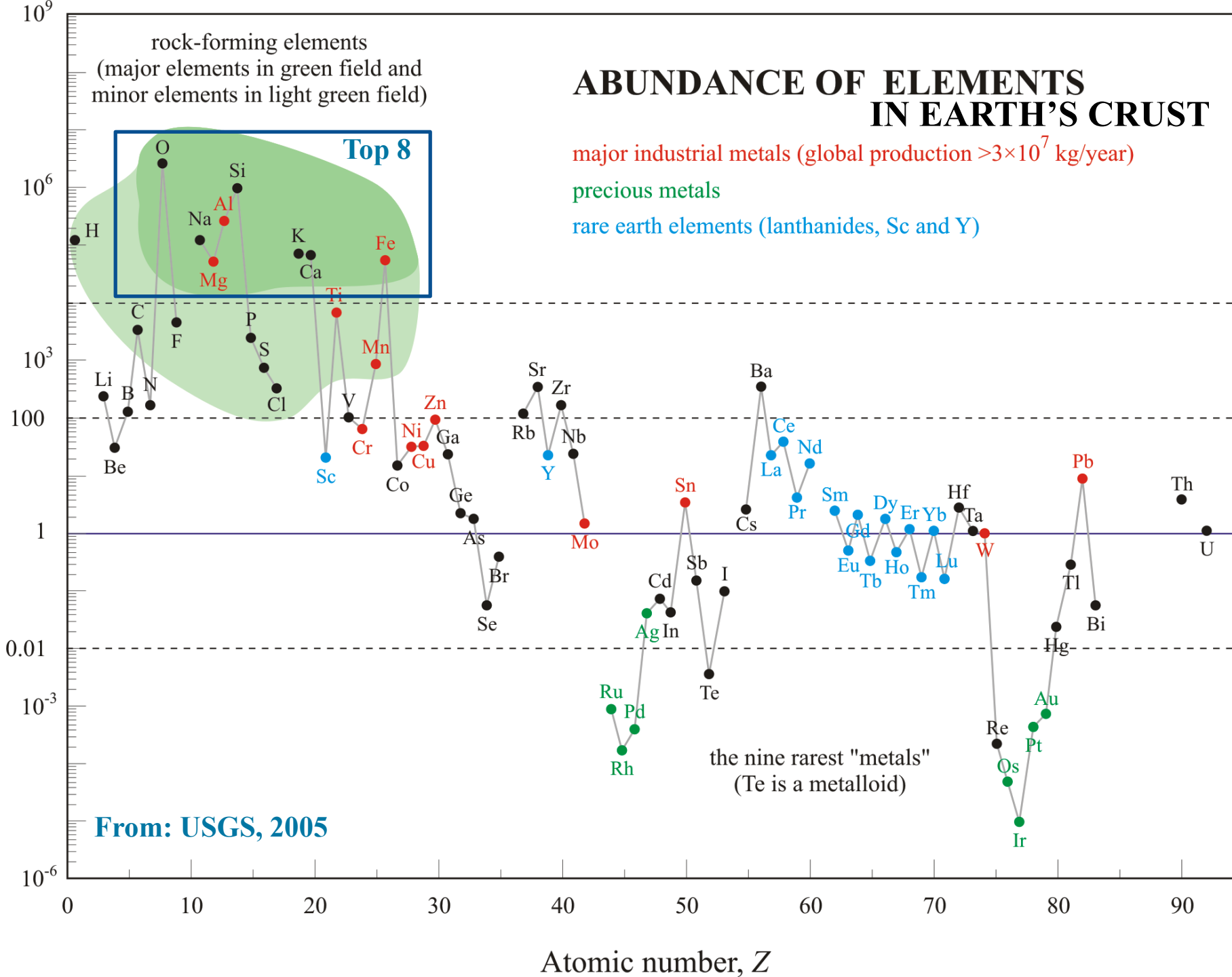
precious metals

rare earth elements (lanthanides, Sc and Y)

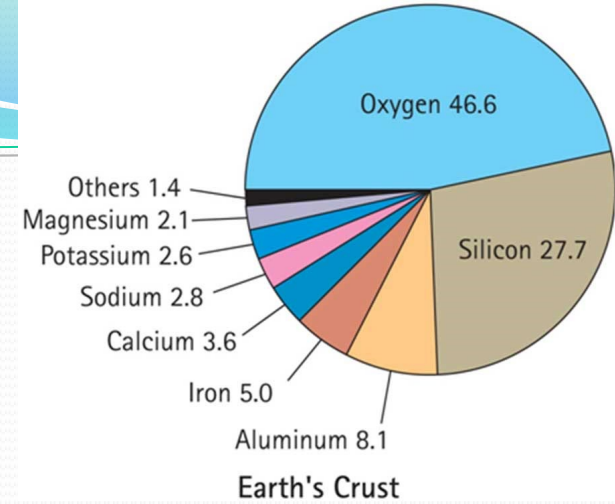
rock-forming elements
(major elements in green field and
minor elements in light green field)



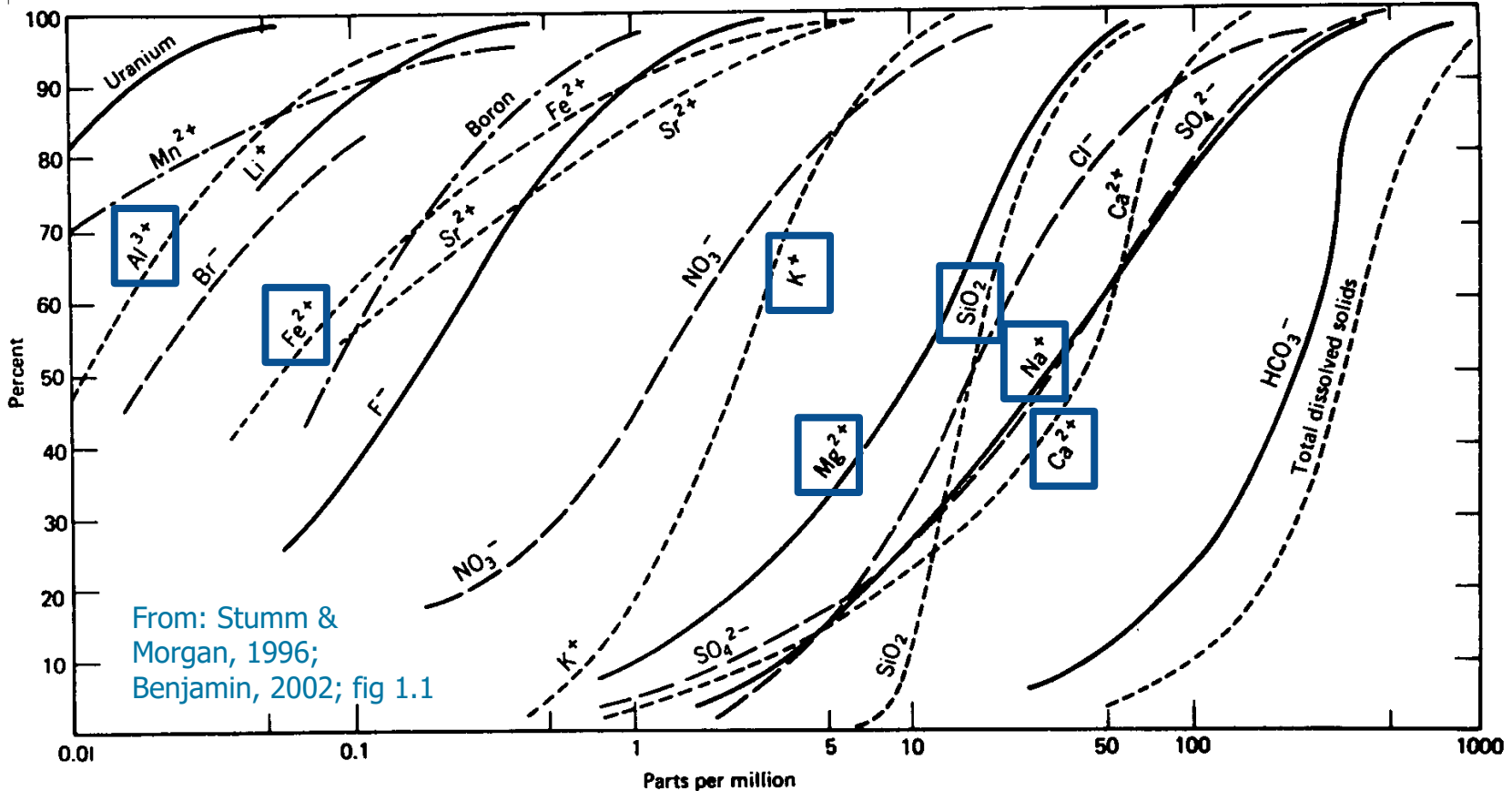
Abundance, atoms of element per million atoms of Si



Abundance of inorganics in fresh water and in earth's crust



Terrestrial water



Solubility Products

- General Equilibrium
 - $A_m B_n(s) \leftrightarrow mA^{+n} + nB^{-m}$
Solid **Cation** **Anion**
- Solubility Product Equation
 - $K_{so} = [A^{+n}]^m [B^{-m}]^n$
 - also sometimes written: K_{sp}
- Example
 - Calcium Carbonate
 - sources: Smith & Martell; S&M, table 7.1 (pg.362-364)

K_{so} and Q

- Reaction Quotient (Q)
 - computed value from actual measurements
 - may not be at thermodynamic equilibrium
 - comparison with K_{sp} will tell you about tendency toward dissolution or precipitation
 - $Q > K_{so}$, then water will precipitate solid phase
 - $Q < K_{so}$, then water will dissolve solid phase
- Example: Calcium Carbonate solubility
 - $Ca^{+2} = 40 \text{ mg/L}$ and $CO_3^{-2} = 100 \text{ mg/L}$ as $CaCO_3$
 - what is Q ?
 - if K_{so} is $10^{-8.34}$, what does this tell us?

Solubility of some simple salts

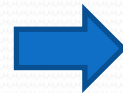
- Barium sulfate



- $K_{\text{so}} = 10^{-9.96} = [\text{Ba}^{+2}][\text{SO}_4^{-2}]$

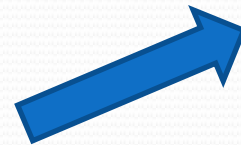
- How much will dissolve, and what will the barium and sulfate concentrations be?

- How much will dissolve in a 1mM solution of Na_2SO_4 ?



$$10^{-9.96} = x(10^{-3} + x)$$
$$= x^2 + 10^{-3}x$$

$$x = \frac{-10^{-3} \pm \sqrt{10^{-6} - 4x10^{-9.96}}}{2}$$
$$= 1.097x10^{-7} = 10^{-6.96}$$



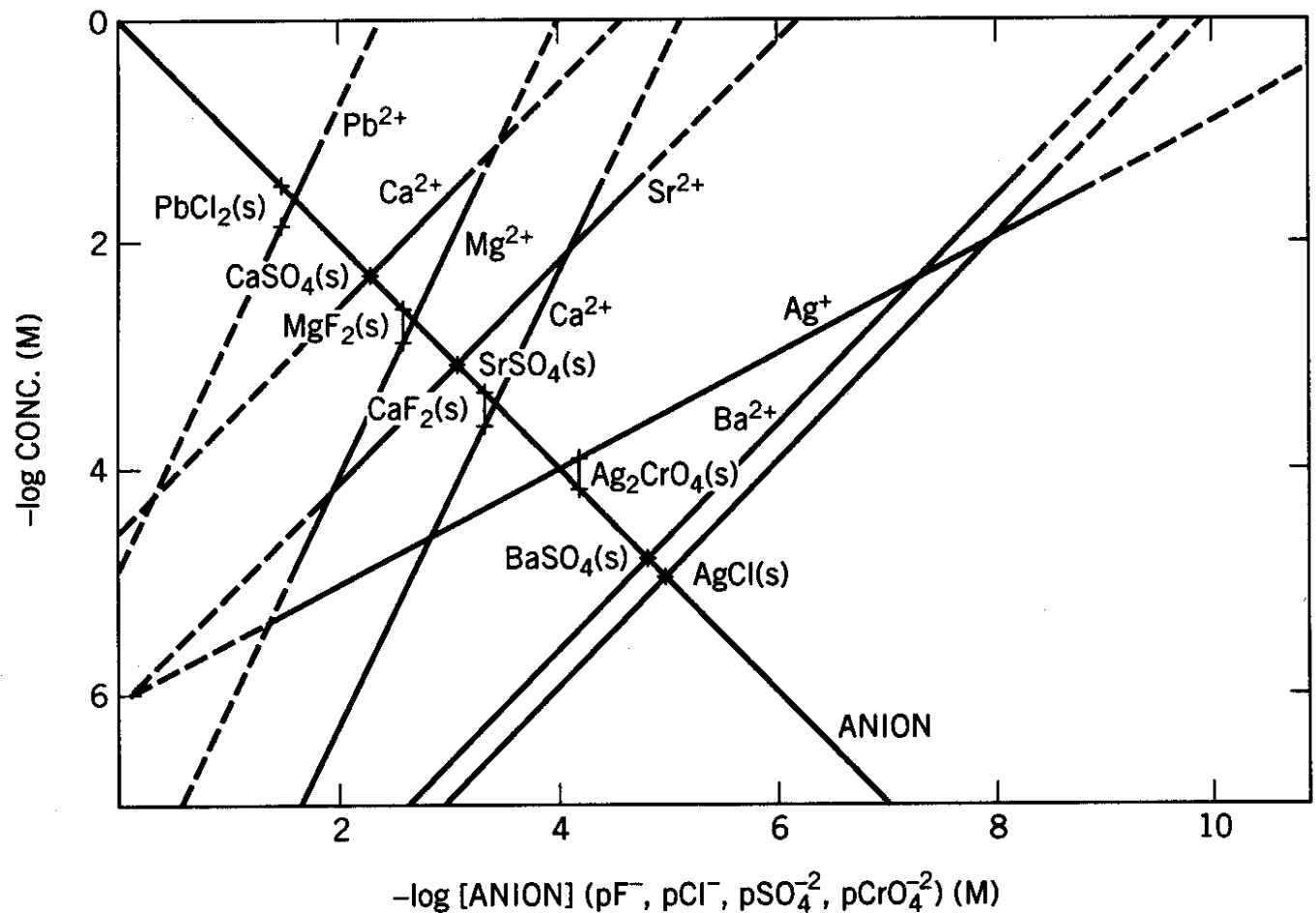
$$10^{-9.96} = x^2$$

$$x = 10^{-4.98}$$

common ion effect

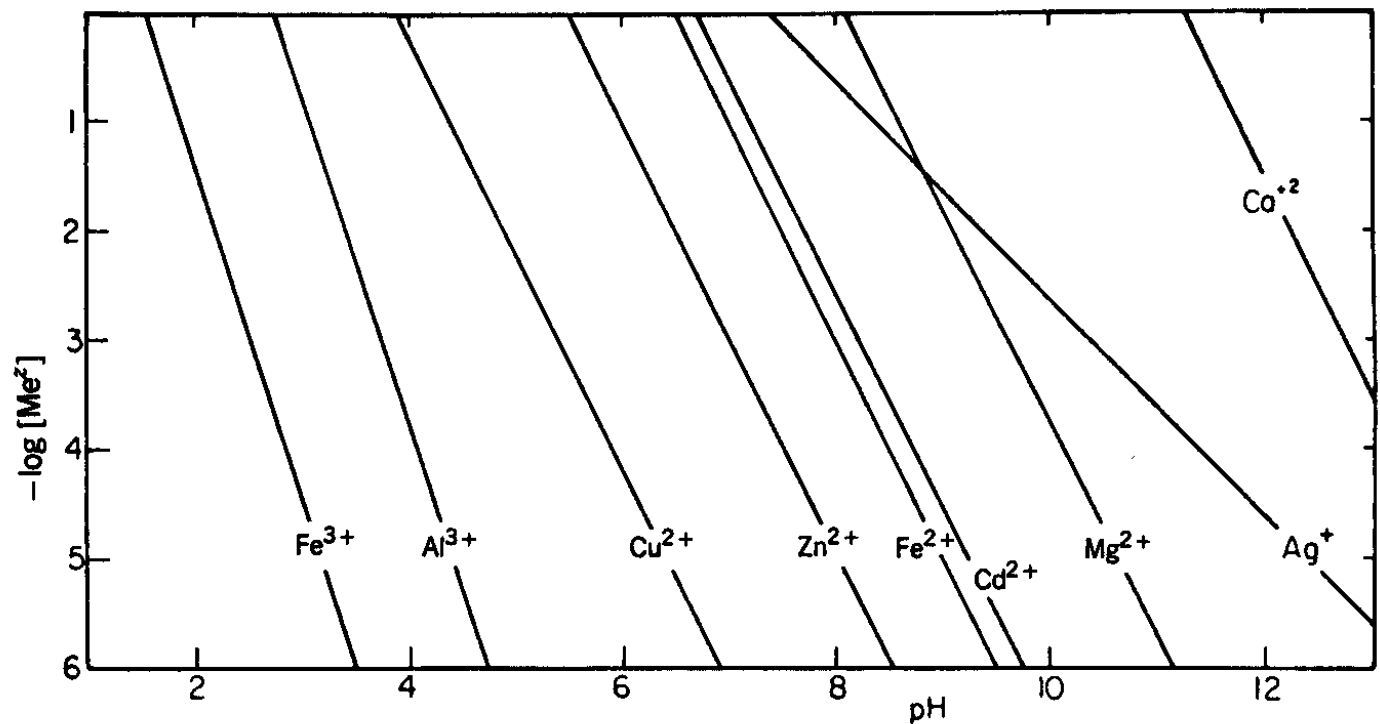
Solubility of “simple” salts

Stumm &
Morgan, 1996,
Figure 7.1, pg.
354



Solubility of oxides & hydroxides

- Does not consider the hydroxometal complexes



Stumm &
Morgan, 1996,
Figure 7.3, pg.
365

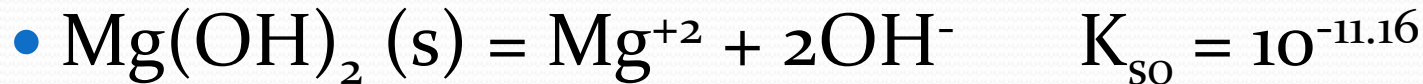
Solubility of metal hydroxides

- Adds complexity
 - hydroxide concentration is controlled by pH and therefore affected by buffering
 - many “hydrolyzing” metals have soluble hydroxide species too
- Example: Magnesium Hydroxide
 - Weakly hydrolyzes
 - Only one soluble hydroxide species
 - Practical: we remove Mg by precipitative softening

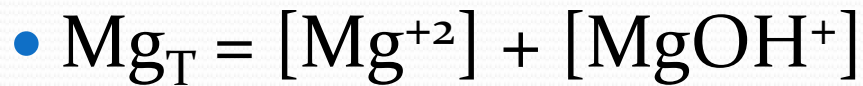
-11.79 Benjamin
 -11.1 Morel
 -10.74 Butler
 -12.9 SM&P
 -11.16 Brezonik
 -11.15 Smith

Magnesium Hydroxide

- Thermodynamics



- Mass Balance



2.56 Stumm
 2.12 Benjamin
 2.6 Morel
 2.58 Smith

Total dissolved concentration:
 does not include precipitated Mg

$\text{Mg}(\text{OH})_2 (s)$ is crystalline Brucite

Smith & Martell

Metal ion	Equilibrium	Hydroxide ion				L ⁻
		Log K 25°, 0.5	Log K 25°, 1.0	Log K 25°, 0	ΔH 25°, 0	
H ⁺	HL/H.L	13.74 ±0.02	13.79 ±0.02	13.997±0.003	-13.34 ±0.01	19.3
		13.78 ^a ±0.01	14.18 ^e ±0.04		-13.55 ^b ±0.05	17.7 ^b
		13.95 ^h			-13.08 ^e ±0.03	21.0 ^e
		13.96 ^d ±0.01			-12.69 ^p	
Li ⁺	ML/M.L		-0.18 ^e	0.36	(0) ^r	(2)
Na ⁺	ML/M.L			-0.2	(0) ^a	(-1)
K ⁺	ML/M.L			-0.5		
Be ²⁺	ML/M.L	8.3 ^h		8.6		
	ML ₂ /M.L ²	(16.5)	(17.5) ^e	(14.4)		
		(16.7) ^h				
	ML ₃ /M.L ³			18.8		
	ML ₄ /M.L ⁴			18.6		
	M ₂ L/M ² .L	10.54	10.95 ^e	(10.0)	-8.9 ^e	20 ^e
		10.68 ^d				
	M ₃ L ₃ /M ³ .L ³	32.41	33.88 ^e	33.1	-24.8 ^e	72 ^e
		32.98 ^d				
	M ₆ L ₈ /M ⁶ .L ⁸			(85)	(-58) ^t	(200)
M.L ² /ML ₂ (s, amorphous)			-21.0			
M.L ² /ML ₂ (s, α)			-21.31			
M.L ² /ML ₂ (s, β)			-21.7			
Mg ²⁺	ML/M.L		1.85 ^e	2.58 ±0.0		
	M ₄ L ₄ /M ⁴ .L ⁴		16.93 ^e	16.3		
	M.L ² /ML ₂ (s)			-11.15 ±0.2		
Ca ²⁺	ML/M.L		0.64 ^e	1.3 ±0.1	2.0	13
	M.L ² /ML ₂ (s)			-5.19 ±0.2	-4.3	-38
Sr ²⁺	ML/M.L		0.23 ^e	0.8 ±0.1	1.2	8

Mg(OH)₂ solid



^a 25°, 0.1; ^b 25°, 0.5; ^d 25°, 2.0; ^e 25°, 3.0; ^h 20°, 0.1; ^p 40°, 0; ^r 15-35°, 0;
^s 0-50°, 0; ^t 0-60°, 1.0 molal

Magnesium Hydroxide

- Tableau

- $[Mg^{+2}] = 10^{16.84}[H^+]^2$ ● ←
- same as:
 - $[Mg^{+2}] = 10^{-11.16}/[OH^+]^2$

	Reactants		
Components	MgOH2 (Brucite)	H+	Log K
Mg+2	1	2	16.84
MgOH+	1	1	5.42
H+	0	1	0

Magnesium Hydroxide II

- From the K_{so} and K_w develop an equation for the free metal in terms of H^+

$$K_{so} = [Mg^{+2}][OH^-]^2$$

$$[Mg^{+2}] = \frac{K_{so}}{[OH^-]^2}$$

$$[Mg^{+2}] = \frac{K_{so}}{K_w^2} [H^+]^2$$

$$[Mg^{+2}] = 10^{16.84} [H^+]^2$$

$$\text{Log}[Mg^{+2}] = 16.84 - 2pH$$

- Then use the K_1 to get an equation for the soluble hydroxide species

$$K_1 = \frac{[MgOH^+]}{[Mg^{+2}][OH^-]}$$

$$[MgOH^+] = K_1 [Mg^{+2}][OH^-]$$

$$= K_1 [Mg^{+2}] \frac{K_w}{[H^+]}$$

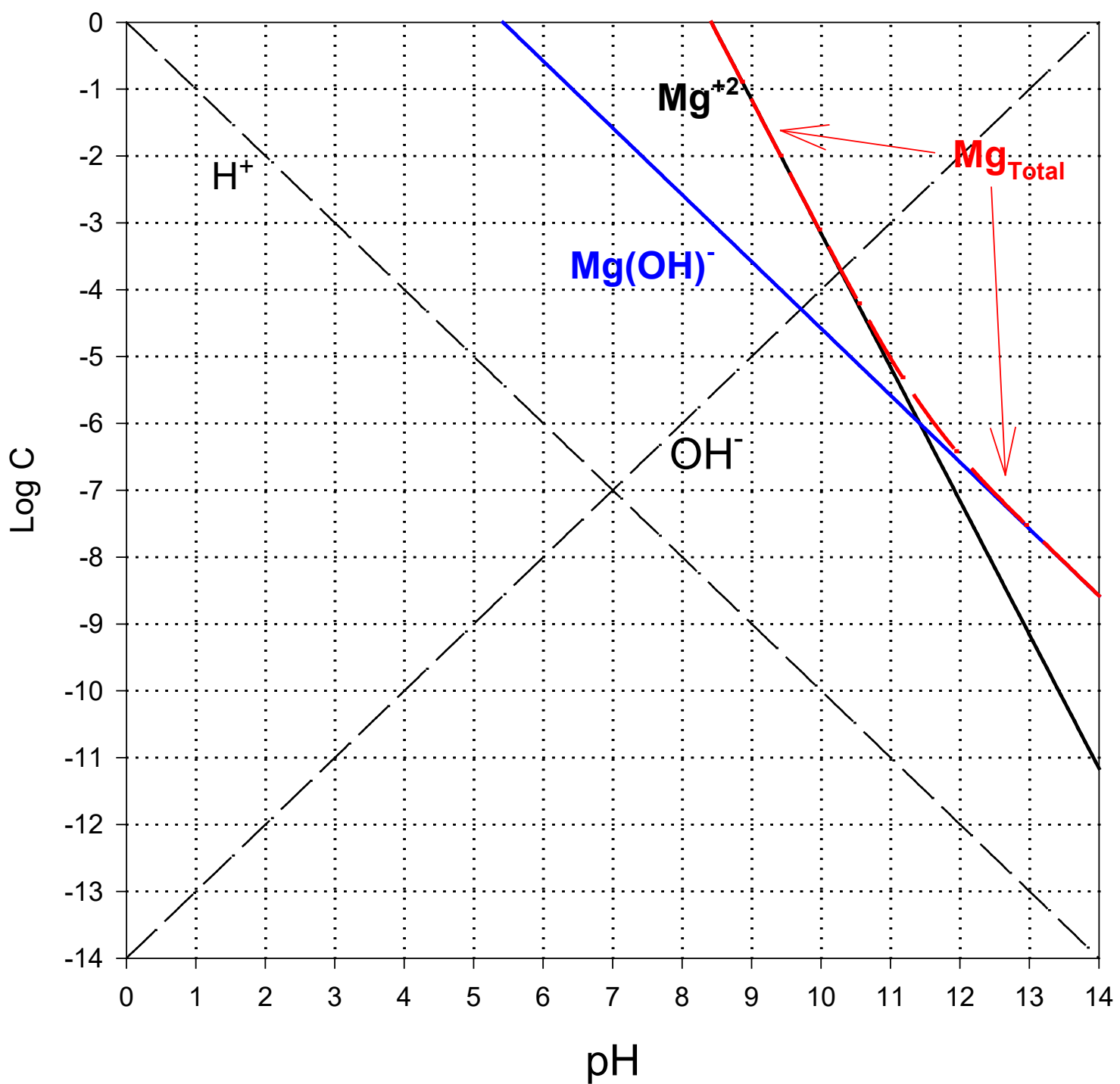
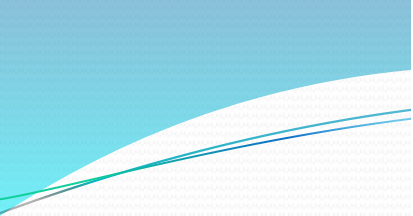
$$= 10^{2.6} \left\{ 10^{16.84} [H^+]^2 \right\} 10^{-14} / [H^+]$$

$$= 10^{5.44} [H^+]$$

$$\text{Log}[MgOH^+] = 5.44 - pH$$

Magnesium Hydroxide III

- Total Magnesium
 - Mg_T
= $[Mg^{+2}] + [MgOH^+]$
 - Follows upper line where lines are well separated
 - Falls 0.3 log units above intersection of any two major species
- Applications
 - Mg is a hardness cation
 - Solubility is controlled by hydroxide precipitate
 - Easily removed by softening at high pH





- To next lecture

Calcium Phosphate

- Providence, RI example
 - See Edwards & Giammar manuscripts