

Ionic Strength Effects

- Ideal or infinite dilution constants (K) are in terms of activity quotients
- These can be factored into molar concentrations and activity coefficients:

activity coefficients:
$$K = \frac{\{H^{+}\}\{B\}}{\{HB\}} \qquad K = \frac{\{H^{+}\}f_{B}[B]}{f_{HB}[HB]}$$

$$= \frac{f_{H^{+}}[H^{+}]f_{B}[B]}{f_{HB}[HB]} \qquad = \left(\frac{f_{B}}{f_{HB}}\right)\frac{\{H^{+}\}[B]}{[HB]}$$

$$= \left(\frac{f_{H^{+}}f_{B}}{f_{HB}}\right)\frac{[H^{+}][B]}{[HB]}$$
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$$CEE 680 \#15$$

Operational Acidity Constants

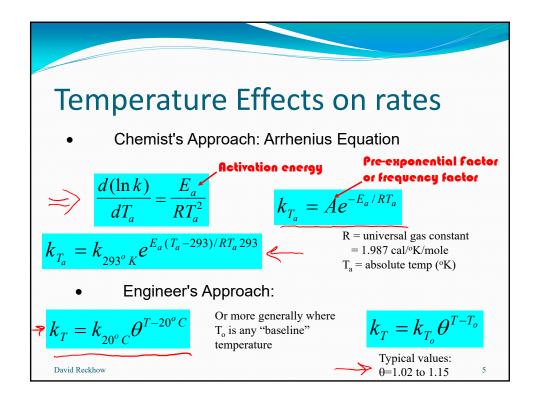
 The common practice of using molar concentrations results in a conditional constant:

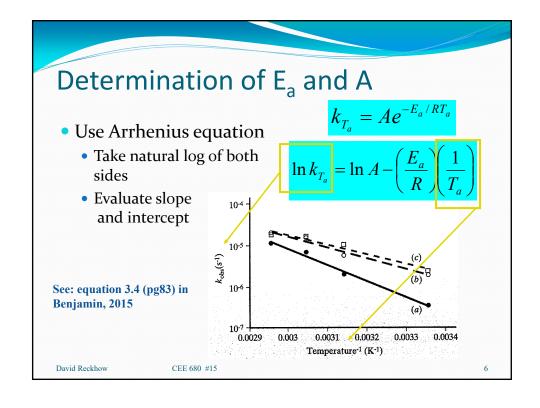
$${}^{c}K \equiv \frac{[H^{+}][B]}{[HB]} = K \left(\frac{f_{HB}}{f_{H^{+}}f_{B}}\right)$$

 And pH measurements generally give us H⁺ activity, so it's often convenient to leave H⁺ in these terms, which results in the mixed acidity constant:

$$K' = \frac{\{H^+\}[B]}{[HB]} = {^C}Kf_{H^+} = \underline{K}\frac{f_{HB}}{f_{R}}$$

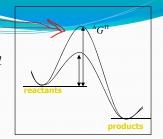
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Catalysis

 A Catalyst enhances rates by providing alternative pathways with lower activation energies



- It is not "consumed" in the reaction
- Homogeneous
 - · Acid/base catalysis
 - Trace metal catalysis
- Heterogeneous
 - Reactions on particle surfaces
 - Reactions mediated by microorganisms (enzymes)
 - Engineered surface catalysis
 - · Catalytic converters, activated carbon

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Sets limits

Chapt 2: Basics

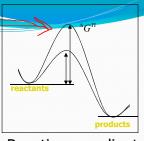
- Thermodynamics
 - Will tell you
 - · which reactions are favorable or "Possible"
 - · composition of systems at equilibrium

Won't tell you

- · how quickly the reactions proceed
- good for systems with constant P & T
 - · Air: 1.0 atm at sea level
 - · Water: 1.0 atm for each additional 10.7 m of water
 - · Earth: wt of overlying rock and soil
- Governing property @ const. T&P is the Gibbs Free Energy
 - for constant T&V, it is the Helmholtz Free Energy

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Reaction coordinate

Gibbs Free Energy

- Combines enthalpy and entropy
 - 1st and 2nd laws of thermodynamics
- Determines whether a reaction is favorable or spontaneous
- Practical form is based on an arbitrary datum
 - the pure and most stable form of each element at standard state

$$^{\Delta}G^{o} = ^{\Delta}H^{o} - T^{\Delta}S^{o}$$

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Standard State

- Standard State
 - Conditions:
 - Unit activity (a=1)
 - Rarely encountered in practice; but easier to base calculations on

About:

1 mole/L for dissolved substances

1 atmosphere for gases

- State variables: ${}^{\Delta}G^{\circ}$, μ°
- Non-standard State
 - Conditions:
 - Non-unit activity, often quite low
 - This is the "real world"
 - State Variables: Δ*G*, μ

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Enthalpy

- A fundamental thermodynamic variable
- enthalpy change is equal to heat of reaction (for systems at constant pressure)
 - ^ΔH<0, heat is given off
 - exothermic
 - [△]H>o, heat is absorbed
 - endothermic
 - ^ΔH can be calculated from standard enthalpies of formation (^ΔH^o_f)
 - available in many texts
 - e.g., Snoeyink & Jenkins, Table 3-1

$$^{\Delta}H^{o} = \sum v_{i}^{\Delta}H_{f}^{o}$$

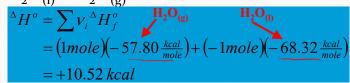
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Example

- Evaporation of water
 - $H_2O_{(l)} = H_2O_{(g)}$



- ^ΔH>o, heat is absorbed
 - endothermic
 - However, this does not tell us if the reaction is favorable, or proceeds spontaneously
 - to answer this we need to know the entropy change

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Thermodynamic Constants for Species of Importance in Water Chemistry (Table 3-1 from Snoeyink & Jenkins) Part I

Species	${}^{\Delta}\overline{H}^{o}_{f}$	${}^{\scriptscriptstyle \Delta} \overline{G}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$	Species	${}^{\vartriangle}\overline{H}^{o}_{f}$	${}^{\scriptscriptstyle{\Delta}}\overline{G}{}^{\scriptscriptstyle{o}}_{\scriptscriptstyle{f}}$
	kcal/mole	kcal/mole		kcal/mole	kcal/mole
Ca ⁺² (aq)	-129.77	-132.18	CO ₃ ⁻² (aq)	-161.63	-126.22
CaC0 ₃ (s), calcite	-288.45	-269.78	CH ₃ COO ⁻ , acetate	-116.84	-89.0
CaO (s)	-151.9	-144.4	H ⁺ (aq)	0	0
C(s), graphite	0	0	$H_{2}\left(g\right)$	0	0
$CO_2(g)$	-94.05	-94.26	Fe ⁺² (aq)	-21.0	-20.30
CO ₂ (aq)	-98.69	-92.31	Fe ⁺³ (aq)	-11.4	-2.52
CH ₄ (g)	-17.889	-12.140	Fe(OH) ₃ (s)	-197.0	-166.0
H ₂ CO ₃ (aq)	-167.0	-149.00	Mn ⁺² (aq)	-53.3	-54.4
HCO ₃ (aq)	-165.18	-140.31	MnO ₂ (s)	-124.2	-111.1

Conversion: 1kcal = 4.184 kJ

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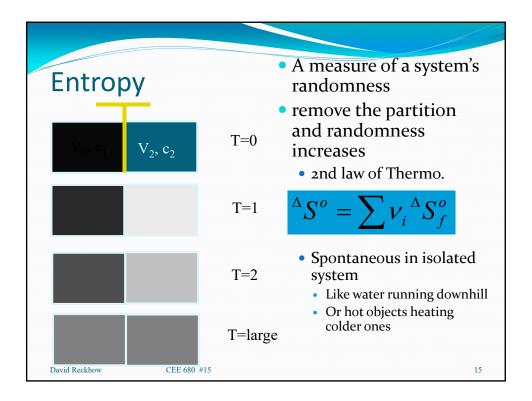
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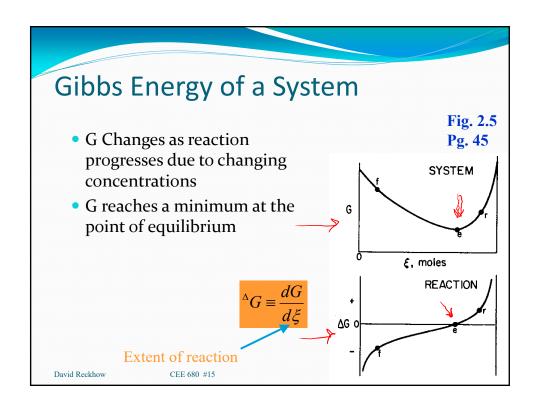
Thermodynamic Constants for Species of Importance in Water Chemistry (Table 3-1 from Snoeyink & Jenkins) Part II

Species	${}^{\Delta}\overline{H}{}^{o}_{f}$	${}^{\scriptscriptstyle \Delta} \overline{G}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$	Species	${}^{\vartriangle}\overline{H}_{f}^{o}$	${}^{\scriptscriptstyle \Delta} \overline{G}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$
	kcal/mole	kcal/mole		kcal/mole	kcal/mole
Mg ⁺² (aq)	-110.41	-108.99	O ₂ (g)	0	0
$Mg(OH)_2(s)$	-221.00	-199.27	OH (aq)	-54.957	-37.595
NO ₃ - (aq)	-49.372	-26.43	H ₂ O (g)	-57.7979	-54.6357
$NH_3(g)$	-11.04	-3.976	H ₂ O (l)	-68.3174	-56.690
NH ₃ (aq)	-19.32	-6.37	SO ₄ -2	-216.90	-177.34
NH ₄ ⁺ (aq)	-31.74	-19.00	HS (aq)	-4.22	3.01
HNO ₃ (aq)	-49.372	-26.41	$H_2S(g)$	-4.815	-7.892
O ₂ (aq)	-3.9	3.93	H ₂ S(aq)	-9.4	-6.54

Conversion: 1kcal = 4.184 kJ

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The G_f Convention

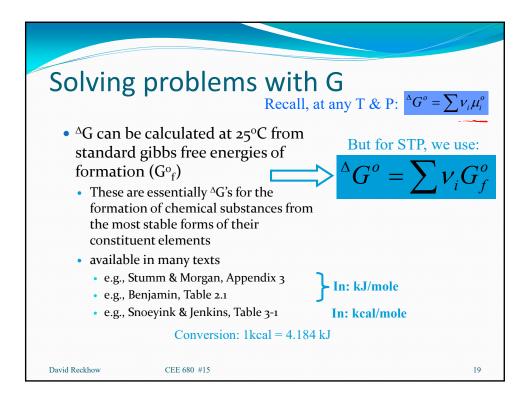
- Since the G_f^o values are essentially △G's for the formation of chemical substances from the "most stable" (reference) forms of their constituent elements
 - The G_f^o values for those most stable elemental forms are zero, by definition
- Examples
 - Zero-valent, Metallic Ag, Al, Fe, Mn, Pb, Zn
 - graphite-C, white-P, rhombic-S
 - diatomic H₂, I₂, N₂, O₂

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Simple examples

Reaction
H_2(g) + S(s) = H_2S(g)
H_2(g) + S(s) = H_2S(g)
G_2(g) + S(s) = SO_2(g)
G_2(g) + S(s) = SO_2(g)
G_3(g) + G_4(g) + G_5(g)
G_4(g) + G_5(g) + G_5(g)
G_2(g) + G_5(g) + G_5(g)
G_2(g) + G_5(g) + G_5(g)
G_3(g) + G_5(g) + G_5(g)
G_4(g) + G_5(g) + G_5(g)
G_5(g) + G_5(g) + G_5(g)
G_5(g) + G_5(g) + G_5(g)
G_7(g) + G_7(g) + G_7(g)
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Ammonia Problem (1/7)

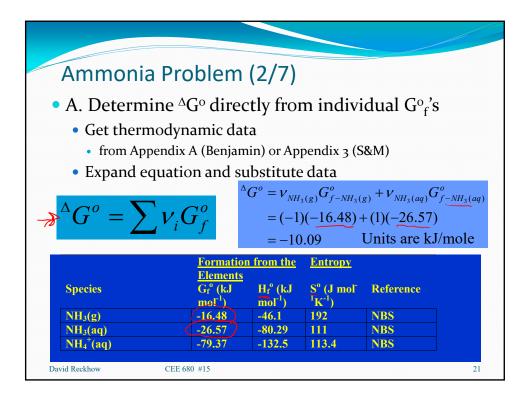
• Determine ${}^{\Delta}G^{o}$ for dissolution of ammonia in water at 25°C

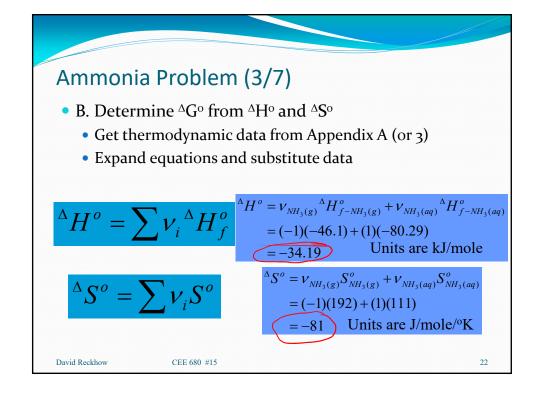
$$NH_3(g) \leftrightarrow NH_3(aq)$$

- Based on example 2.5 in text
- Two approaches
 - A. Determine ^ΔG^o directly from individual G^o_f's
 - · The easiest way
 - B. Determine ${}^{\Delta}G^{\circ}$ from ${}^{\Delta}H^{\circ}$ and ${}^{\Delta}S^{\circ}$

$$^{\Delta}G^{o} = ^{\Delta}H^{o} - T^{\Delta}S^{o}$$

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Ammonia Problem (4/7)

• Now combine and solve for △G°

$$^{\Delta}G^{o} = ^{\Delta}H^{o} - T^{\Delta}S^{o}$$

$$= (-34.19) - (273.16 + 25)(-81)(\frac{1kJ}{1000J})$$

$$= -10.04$$
Units are kJ/mole

- Conclusion: reaction is spontaneous since △G° <o
- Lingering question: what actually happens when we're not at standard state conditions (i.e., when activity isn't equal to one)?

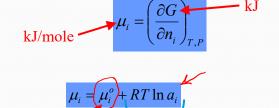
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Chemical Potential

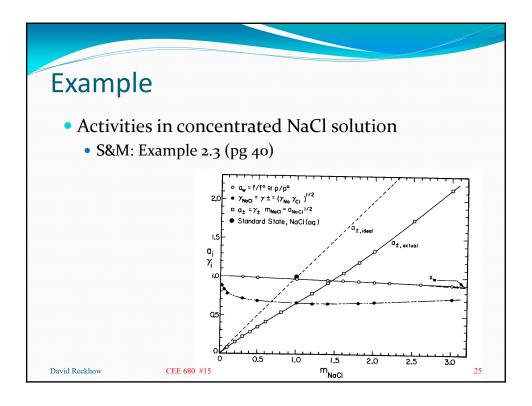
- Like a Gibbs Free Energy normalized per mole
- a function of activity and temperature

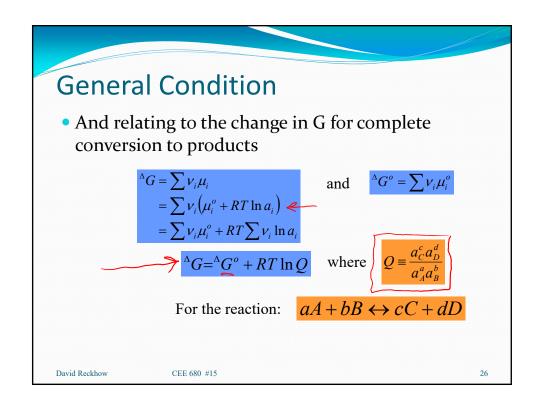


Standard state (unit activity)

This term corrects for the fact that we're not at unit activity

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Ammonia problem (5/7)

- Now lets see what the ^ΔG is for the following nonstandard conditions
 - $[NH_3(aq)] = 10^{-3} M$
 - $p_{NH_3} = 10^{-4}$ atm
- Now we need to determine Q
 - Recall the reaction:

 $NH_3(g) \leftrightarrow NH_3(aq)$

• So:

$$Q = \frac{a_{NH_3(aq)}^1}{a_{NH_3(g)}^1} \approx \boxed{10^{-3} \\ 10^{-4}} = 10$$

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Ammonia problem (6/7)

R=1.987 x10⁻³ kcal/mole °K =8.314 x10⁻³ kJ/mole °K

Now substitute back into the equation for [△]G

$$^{\Delta}G = ^{\Delta}G^{0} + RT \ln Q$$

$$= -10.04 + (0.008314)(273.16 + 25) \ln(10)$$

$$= -4.33$$
Units are kJ/mole

- Conclusion: the reaction is still spontaneous at these non-standard concentrations
 - i.e., the reaction will proceed toward the right
- Another lingering question: how far to the right will it proceed before it reaches equilibrium and stops?
 - To answer this we need to determine "K"

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Equilibrium Quotients

- at Equilibrium [△]G=0, so:
 - and:

$$\underline{^{\Delta}G^{\circ} = -RT \ln K}$$

$$= -2.303RT \log K$$

• or:

$$\log K = -\frac{{}^{\Delta}G^{o}}{2.303RT}$$

 $0=^{\Delta}G^{\circ}+RT\ln K$

Where K is defined as the quotient (Q) at equilibrium and is generally referred to as the "equilibrium constant"

$$K \equiv \frac{a_C^c a_D^d}{a_A^a a_B^b}$$
, at equilibrium

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Ammonia problem (7/7)

R=1.987 x10⁻³ kcal/mole °K =8.314 x10⁻³ kJ/mole °K

 To determine the equilibrium position of ammonia dissolution, we need the equilibrium constant, K

$$\log K = -\frac{{}^{\Delta}G^{\circ}}{2.303RT}$$

$$= -\frac{-10.04}{2.303(0.008314)(273.16 + 25)}$$

$$= 1.76$$

 $K = 10^{1.76}$ = 57.4

• So as we approach equilibrium, Q will approach the value of K, which is 57.4

$$Q = \frac{a_{NH_3(aq)}^1}{a_{NH_3(g)}^1} \cong \frac{10^{-3}}{10^{-4}} = 10$$

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Quotients (cont.)

 more generally, for non-equilibrium conditions, we can combine:

$$^{\Delta}G = ^{\Delta}G^{o} + RT \ln Q$$

$$= -RT \ln K + RT \ln Q$$

$$= RT \ln \left(\frac{Q}{K}\right)$$

 $^{\Delta}G = 2.303RT \log \left(\frac{Q}{K}\right)$

- and if,
 - ${}^{\Delta}G$ <0, (Q/K)<1, and equilibrium lies to the right
 - ${}^{\Delta}G>0$, (Q/K)>1, and equilibrium lies to the left
 - [∆]G=o, (Q/K)=1, and system is at equilibrium

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Chromium Example (1/6)

Hexavalent Cr is now a big regulatory issue

Historically, chromium (Cr) has been used in numerous industrial processes, including leather tanning and metal plating operations. In these applications, if the water is mildly acidic, the Cr is typically present as bichromate ($HCrO_4^-$) and/or dichromate ($Cr_2O_7^{2^-}$) ions. These ions can be interconverted by the reaction

$$2HCrO_4^- \leftrightarrow Cr_2O_7^{2-} + H_2O$$

The standard Gibbs energies of formation of $HCrO_4^-$, $Cr_2O_7^{2-}$, and H_2O are -764.8, -1301, and -237.18 kJ/mol, respectively.

- a. Compute the equilibrium constant for the conversion of $HCrO_4^-$ to $Cr_2O_4^{\ 2-}$.
- b. Compute G_{tot} as a function of the relative amounts of HCrO_4^- and $\text{Cr}_2\text{O}_7^{2-}$ in a system containing $10^{-1}\,M$ total dissolved chromium ($c_{\text{Cr,tot}}$). Compare the condition of minimum chemical potential energy with the equilibrium condition as specified by the equilibrium constant. Assume all activity coefficients are 1.0.
- c. Compute $\Delta \overline{G}_r$ as a function of the $HCrO_4^-$ concentration for the solution described in part (b).

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Example 4.10 (pg 188) from Benjamin 2015 CEE Mathiple 2.10 (pg 111) in Benjamin, 2002

Chromium Example (2/6)

Solution

a. The reaction of interest is $2HCrO_4^- \leftrightarrow Cr_2O_7^{2-} + H_2O$, for which the standard Gibbs energy of reaction is

$$\Delta \vec{G}_r^{\text{o}} = \vec{G}_{\text{Cr},\text{O}_7}^{\text{o}} + \vec{G}_{\text{H},\text{O}}^{\text{o}} - 2\vec{G}_{\text{HCrO}_4}^{\text{o}}$$
$$\Delta \vec{G}_r = [-1301 + (-237.18) - 2(-764.8)] \text{ kJ/mol} = -8.58 \text{ kJ/mol}$$

Applying Equation (2.87), we obtain

$$\log K = -\frac{{}^{\Delta}G^{o}}{2.303RT}$$

$$\log K_{\rm eq} = -\frac{-8.58 \text{ kJ/mol}}{5.71 \text{ kJ/mol}} = +1.51$$

$$K_{eq} = 32.5$$

b. The total Gibbs energy of the solution is the sum of the Gibbs energy contributions of the various constituents:

$$G_{\text{tot}} = n_{\text{H},\text{O}}(\overline{G}_{\text{H},\text{O}}^{\text{O}} + RT \ln a_{\text{H},\text{O}}) + n_{\text{HCrO}_4^-}(\overline{G}_{\text{HCrO}_4^-}^{\text{O}} + RT \ln a_{\text{HCrO}_4^-}) + n_{\text{Cr}_2\text{O}_7^{\text{-}}}(\overline{G}_{\text{Cr},\text{O}_7^{\text{-}}}^{\text{O}} + RT \ln a_{\text{Cr}_2\text{O}_7^{\text{-}}})$$
(2.90)

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Example 2.10 from (pg 111): Benjamin, 2002 CEE 680 #15

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Chromium Example (3/6)

where n_i is the number of moles of i in the system. Assuming that the system volume (V) is independent of the distribution of Cr, Vc_i can be substituted for n_i for each species. Substituting molar concentrations for the activities of the chromium species, and setting the activity of water equal to its mole fraction $(a_{\rm H_2O} = c_{\rm H_2O}/\sum c_i)$, we obtain 13

$$G_{\text{tot}} = Vc_{\text{H}_2\text{O}} \left(\overline{G}_{\text{H}_2\text{O}}^{\text{o}} + RT \ln \frac{c_{\text{H}_2\text{O}}}{\sum c_i} \right) + Vc_{\text{HCrO}_4} (\overline{G}_{\text{HCrO}_4}^{\text{o}} - + RT \ln c_{\text{HCrO}_4})$$

$$+ Vc_{\text{Cr}_2\text{O}_7}^{\text{2-}} (\overline{G}_{\text{Cr}_2\text{O}_7}^{\text{O}} + RT \ln c_{\text{Cr}_2\text{O}_7}^{\text{2-}})$$
(2.91)

$$\frac{G_{\text{tot}}}{V} = c_{\text{H}_2\text{O}} \left(\overline{G}_{\text{H}_2\text{O}}^{\text{o}} + RT \ln \frac{c_{\text{H}_2\text{O}}}{\sum c_i} \right) + c_{\text{HCrO}_4^-} (\overline{G}_{\text{HCrO}_4^-}^{\text{o}} + RT \ln c_{\text{HCrO}_4^-})
+ c_{\text{Cr}_2\text{O}_2^{2-}} (\overline{G}_{\text{Cr}_2\text{O}_2^{2-}}^{\text{o}} + RT \ln c_{\text{Cr}_2\text{O}_2^{2-}})$$
(2.92)

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Example 4.10 (pg 188) from Benjamin 2015 CEE 680 #15

Chromium Example (4/6)

The concentrations of $HCrO_4^-$ and $Cr_2O_7^{2-}$ are related to each other by stoichiometry. Furthermore, since 1 L of solution contains 55.56 mol of water, the mole fraction of water can be computed as a function of the concentration of either of the other species:

$$c_{\text{Cr}_2\text{O}_7^{2^-}} = 0.5(c_{\text{Cr},\text{tot}} - c_{\text{HCrO}_4^-}) = 0.5(0.10 - c_{\text{HCrO}_4^-})$$

$$a_{\text{H}_2\text{O}} = \frac{55.56}{55.56 + c_{\text{HCrO}_4^-} + c_{\text{CrO}_7^{2^-}}} = \frac{55.56}{55.56 + c_{\text{HCrO}_4^-} + 0.5(0.10 - c_{\text{HCrO}_4^-})}$$

$$= \frac{55.56}{55.56 + 0.05 + 0.5c_{\text{HCrO}_4^-}}$$
(2.94)

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Example 2.10 from (pg 111): Benjamin, 2002 CEE 680 #15

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Chromium Example (5/6)

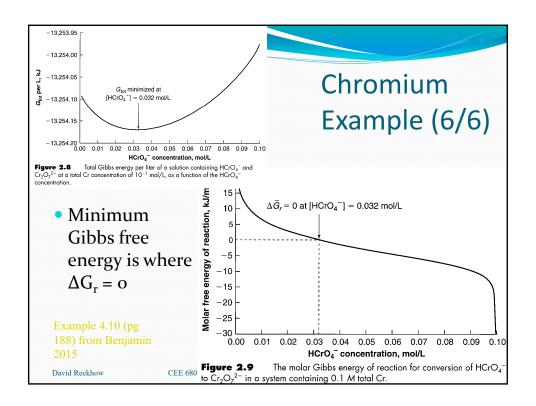
Substitution of Equations (2.93) and (2.94) into (2.92) yields a long but not complex expression for $G_{\rm tot}$ per unit volume of solution in terms of a single variable, $c_{\rm HCrO_4}$. The exact value of $c_{\rm HCrO_4}$ —where $G_{\rm tot}/V$ is minimized could be found by differentiation with respect to $c_{\rm HCrO_4}$ —. A plot of $G_{\rm tot}/V$ versus $c_{\rm HCrO_4}$ —(Figure 2.8) indicates that the point of minimum Gibbs energy in the system (and hence the equilibrium condition) is at $c_{\rm HCrO_4}$ —=0.0320 mol/L, corresponding to $c_{\rm Cr_2O_7^{2-}}=0.034$ mol/L. The activity (mole fraction) of water under these conditions is close to 0.999, so the activity quotient for the reaction is

$$Q = \frac{\{\text{Cr}_2\text{O}_7^{\ 2^-}\}\{\text{H}_2\text{O}\}}{\{\text{HCr}\text{O}_4^{\ -}\}^2} = \frac{0.034(0.999)}{(0.032)^2} = 33.2 \qquad \ln Q = 3.50$$

The computed value of Q is essentially identical to the value of $K_{\rm eq}$ computed in part (a). That is, the activity ratio indicates that when the total chemical potential energy of the system is minimized, Q=K, i.e., the reaction is at equilibrium. (The small difference between the computed values of Q and K is due to round-off error.)

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Example 4.10 (pg 188) from Benjamin 2015 CEE 680 #15



Alternative Direct Calculation

Assume standard activity for water

$$K = \frac{\left[Cr_2O_7^{-2}\right]}{\left[HCrO_4^{-}\right]^2}$$

Combine equilibrium and mass balance equations

$$Cr_{total} = 0.1 = [HCrO_4^-] + 2[Cr_2O_7^{-2}]$$

• Set bichromate = x

$$2[Cr_2O_7^{-2}]=0.1-x$$

$$K = 32.5 = \frac{\left[Cr_2O_7^{-2}\right]}{\left[HCrO_4^{-1}\right]^2} = \frac{0.05 - 0.5x}{x^2}$$
$$32.5x^2 + 0.5x - 0.05 = 0$$

• And using the quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = \frac{-0.5 \pm \sqrt{0.25 - 6.5}}{65} = 0.032278$$

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Ionic Species & Redox

- Conventions
 - $G_f^o = o$, for H_2
 - $G_f^{\circ} = 0$, for H^+
 - this makes the hydrogen oxidation half reaction a reference point for Redox
 - for: ${}^{1}/_{2}H_{2(g)} = H^{+} + e^{-}$, ${}^{\Delta}G = o$
- oxidations and reductions
 - must be coupled
 - we only concern ourselves with the differences in [△]G for the two half reactions

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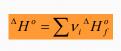
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Temperature Effects on K

- Need [△]H (enthalpy change)
 - ^ΔH < 0, exothermic (heat evolved)
 - ^ΔH > 0, endothermic (heat absorbed)
- The Van't Hoff Equation:

$$\log \frac{K_2}{K_1} = \frac{{}^{\Delta}H^o(T_2 - T_1)}{2.303RT_2T_1}$$

• recall that:

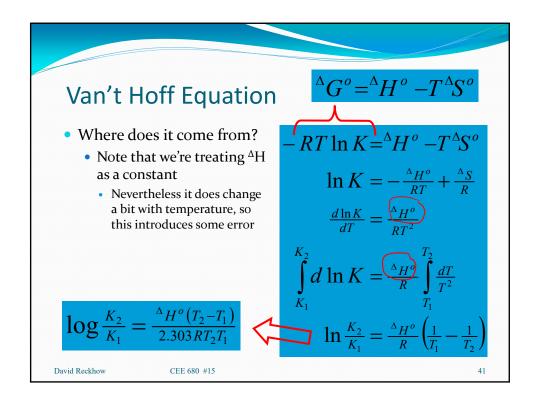


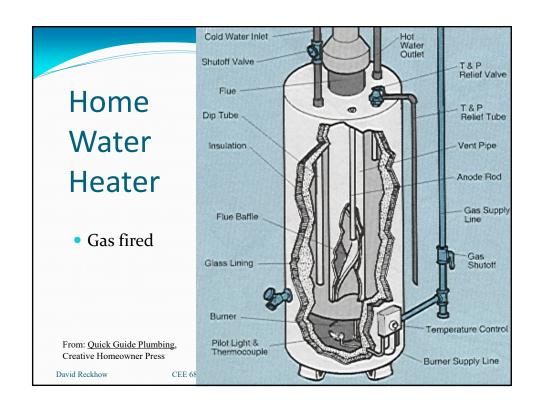
Log K

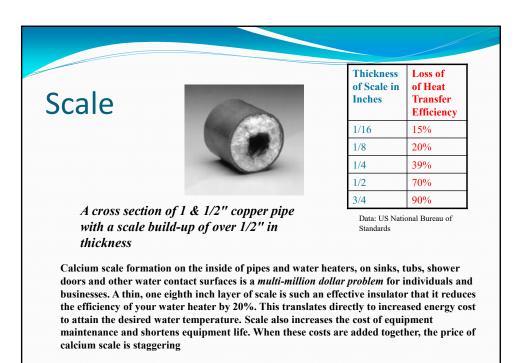


1/T

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Example Problem

- Water is at equilibrium with calcium carbonate at 25°C. It enters a house at 15°C, then is heated to 60°C in a water heater.
 - Is the water supersaturated as it

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- A. enters the house?
- B. leaves the water heater?
- Solution to A.
 - 1. Calculate [△]G^o
 - 2. Determine K₁ at 25°C
 - 3. Determine [△]H^o
 - 4. Determine K₂ at 15°C

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Solution

- At neutral pH: $CaCO_{3(s)} + H^{+} = HCO_{3}^{-} + Ca^{+2}$
 - 1. Calculate [△]G^o
 - =-140.31-132.18-(-269.78) = -2.71 kcal
 - 2. Determine K₁ at 25°C
 - ΔG° =-RTlnK = -2.303RT*logK
 - -2.71=-2.303(0.001987)298*logK =-1.364logK
 - log K =1.99; K=10^{1.99}
 - 3. Determine [∆]H^o
 - =-165.18-129.77-(-288.345) = -6.5 kcal
 - 4. Determine K, at 15°C
 - $\log (K_2/10^{1.99}) = -6.5(288-298)/2.303(0.001987)288(298)=0.1655$
 - $\log K_2 = 2.156$
 - $K_2 = 10^{2.16}$

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Thermodynamic Constants for Species of Importance in Water Chemistry (Table 3-1 from Snoeyink & Jenkins) Part I

Species	${}^{\scriptscriptstyle{\Delta}}\overline{H}{}^{\scriptscriptstyle{o}}_{\scriptscriptstyle{f}}$	${}^{\scriptscriptstyle \Delta} \overline{\overline{G}}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$	Species	${}^{\Delta}\overline{H}^{o}_{f}$	${}^{\scriptscriptstyle \Delta} \overline{G}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$
	kcal/mole	kcal/mole		kcal/mole	kcal/mole
Ca ⁺² (aq)	-129.77	-132.18	CO ₃ ⁻² (aq)	-161.63	-126.22
CaC0 ₃ (s), calcite	-288.45	-269.78	CH ₃ COO ⁻ , acetate	-116.84	-89.0
CaO (s)	-151.9	-144.4	H ⁺ (aq)	0	0
C(s), graphite	0	0	H ₂ (g)	0	0
CO ₂ (g)	-94.05	-94.26	Fe ⁺² (aq)	-21.0	-20.30
CO ₂ (aq)	-98.69	-92.31	Fe ⁺³ (aq)	-11.4	-2.52
CH ₄ (g)	-17.889	-12.140	Fe(OH) ₃ (s)	-197.0	-166.0
H ₂ CO ₃ (aq)	-167.0	-149.00	Mn ⁺² (aq)	-53.3	-54.4
HCO ₃ (aq)	-165.18	-140.31	$MnO_2(s)$	-124.2	-111.1

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Thermodynamic Constants for Species of Importance in Water Chemistry (Table 3-1 from Snoeyink & Jenkins) Part II

Species	${}^{\scriptscriptstyle \Delta}\overline{H}{}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$	${}^{\scriptscriptstyle \Delta} \overline{G}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$	Species	${}^{\Delta}\overline{H}^{o}_{f}$	${}^{\scriptscriptstyle \Delta} \overline{G}^{\scriptscriptstyle o}_{\scriptscriptstyle f}$
	kcal/mole	kcal/mole		kcal/mole	kcal/mole
Mg^{+2} (aq)	-110.41	-108.99	$O_2(g)$	0	0
$Mg(OH)_2(s)$	-221.00	-199.27	OH (aq)	-54.957	-37.595
NO ₃ (aq)	-49.372	-26.43	H ₂ O (g)	-57.7979	-54.6357
$NH_3(g)$	-11.04	-3.976	H ₂ O (1)	-68.3174	-56.690
NH ₃ (aq)	-19.32	-6.37	SO ₄ -2	-216.90	-177.34
NH_4^+ (aq)	-31.74	-19.00	HS (aq)	-4.22	3.01
HNO ₃ (aq)	-49.372	-26.41	$H_2S(g)$	-4.815	-7.892
O ₂ (aq)	-3.9	3.93	H ₂ S(aq)	-9.4	-6.54

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Solution (cont.)

- Repeat step #4 for 60°C.
 - 4. Determine K₂ at 60°C
 - $\log (K_3/10^{1.99}) = -6.5(333-298)/2.303(0.001987)333(298) = -0.5$
 - $\log K_3 = 1.49$
 - $K_3 = 10^{1.49}$
- Compare K₁ and K₂ and K₃
 - what does this tell you about possible precipitation?
 - As temp increases, solubility decreases
 - This is an exothermic reaction, so rising temp drives reaction to the left

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Le Chatelier's Principle

- A system at equilibrium, when subject to a perturbation, responds in a way that tends to minimize its effect
 - If $^{\Delta}$ H>o (endothermic), dlnK/dT >o, and K \uparrow as T \uparrow
 - if you heat endothermic reaction they will go further to the right
 - If ${}^{\Delta}H$ <0 (exothermic), dlnK/dT <0, and K \Downarrow as T \uparrow
 - if you heat exdothermic reaction they will go back to the left

$$\frac{d\ln K}{dT} = \frac{{}^{\Delta}H^o}{RT^2}$$

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Log K vs 1/T: based on empirical data

- Stepwise acid dissociation (1st or 2nd constant)
 - Note reciprocal T scale is descending, so lines should be sloping upward

