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# CEE 680: Water Chemistry

Lecture #14

Acids & Bases: Polyprotics  
Benjamin, Chapter 4  
(Stumm & Morgan, Chapt.3)

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## Hydrogen Sulfide example

$$\alpha_0 \equiv \frac{[H_2S]}{C_T} = \frac{1}{1 + \frac{K_1}{[H^+]} + \frac{K_1 K_2}{[H^+]^2}}$$

	Slope	Intercept
<ul style="list-style-type: none"> <li>• Lines for H<sub>2</sub>S               <ul style="list-style-type: none"> <li>• Low pH (pH &lt;&lt; pK<sub>1</sub>, or [H<sup>+</sup>] &gt;&gt; K<sub>1</sub>)                   <ul style="list-style-type: none"> <li>• α<sub>0</sub> = 1 or [H<sub>2</sub>S] = C<sub>T</sub></li> <li>• log[H<sub>2</sub>S] = log C<sub>T</sub></li> </ul> </li> <li>• Intermediate pH (pK<sub>1</sub> &lt;&lt; pH &lt;&lt; pK<sub>2</sub>, or K<sub>1</sub> &gt;&gt; [H<sup>+</sup>] &gt;&gt; K<sub>2</sub>)                   <ul style="list-style-type: none"> <li>• α<sub>0</sub> = [H<sup>+</sup>]/K<sub>1</sub> or [H<sub>2</sub>S] = C<sub>T</sub>[H<sup>+</sup>]/K<sub>1</sub></li> <li>• log[H<sub>2</sub>S] = log C<sub>T</sub> + pK<sub>1</sub> - pH</li> </ul> </li> <li>• High pH (pK<sub>2</sub> &lt;&lt; pH, or K<sub>2</sub> &gt;&gt; [H<sup>+</sup>])                   <ul style="list-style-type: none"> <li>• α<sub>0</sub> = [H<sup>+</sup>]<sup>2</sup>/K<sub>1</sub>K<sub>2</sub> or [H<sub>2</sub>S] = C<sub>T</sub>[H<sup>+</sup>]<sup>2</sup>/K<sub>1</sub>K<sub>2</sub></li> <li>• log[H<sub>2</sub>S] = log C<sub>T</sub> + pK<sub>1</sub> + pK<sub>2</sub> - 2pH</li> </ul> </li> </ul> </li> </ul>	0	Log C <sub>T</sub>
	-1	7 + log C <sub>T</sub>
	-2	21 + log C <sub>T</sub>

H<sub>2</sub>S ⇌ HS<sup>-</sup> ⇌ S<sup>-2</sup>

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### Hydrogen Sulfide example

$$\alpha_1 \equiv \frac{[HA^-]}{C_T} = \frac{1}{\frac{[H^+]}{K_1} + 1 + \frac{K_2}{[H^+]}}$$

	Slope	Intercept
<ul style="list-style-type: none"> <li>• Lines for HS<sup>-</sup> <ul style="list-style-type: none"> <li>• Low pH (pH &lt;&lt; pK<sub>1</sub>, or [H<sup>+</sup>] &gt;&gt; K<sub>1</sub>)                             <ul style="list-style-type: none"> <li>• <math>\alpha_1 = K_1/[H^+]</math> or <math>[HS^-] = C_T K_1/[H^+]</math></li> <li>• <math>\log[HS^-] = \log C_T - pK_1 + pH</math></li> </ul> </li> <li>• Intermediate pH (pK<sub>1</sub> &lt;&lt; pH &lt;&lt; pK<sub>2</sub>, or K<sub>1</sub> &gt;&gt; [H<sup>+</sup>] &gt;&gt; K<sub>2</sub>)                             <ul style="list-style-type: none"> <li>• <math>\alpha_1 = 1</math> or <math>[HS^-] = C_T</math></li> <li>• <math>\log[HS^-] = \log C_T</math></li> </ul> </li> <li>• High pH (pK<sub>2</sub> &lt;&lt; pH, or K<sub>2</sub> &gt;&gt; [H<sup>+</sup>])                             <ul style="list-style-type: none"> <li>• <math>\alpha_1 = [H^+]/K_2</math> or <math>[HS^-] = C_T [H^+]/K_2</math></li> <li>• <math>\log[HS^-] = \log C_T + pK_2 - pH</math></li> </ul> </li> </ul> </li> </ul>	+1	-7+Log C <sub>T</sub>
	0	log C <sub>T</sub>
	-1	14+log C <sub>T</sub>

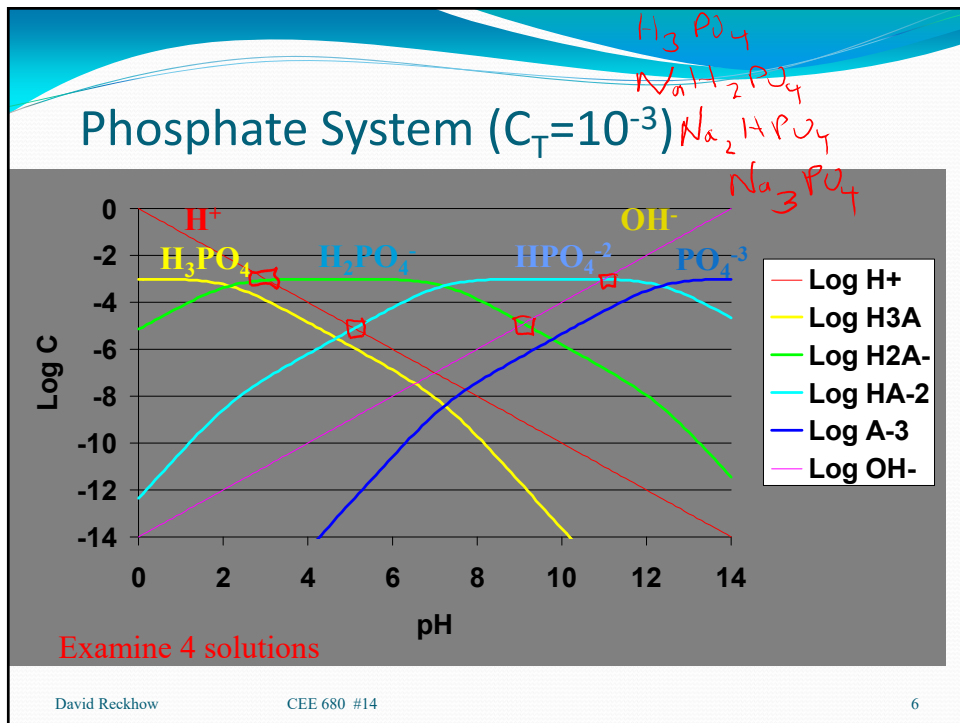
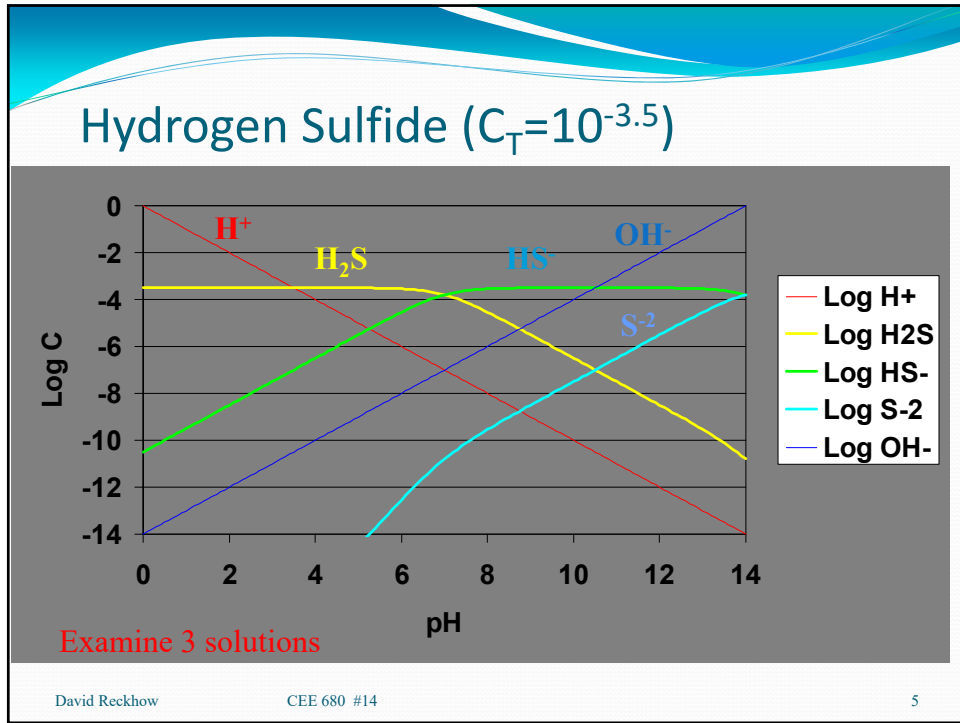
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### Hydrogen Sulfide example

$$\alpha_2 \equiv \frac{[A^{-2}]}{C_T} = \frac{1}{\frac{[H^+]^2}{K_1 K_2} + \frac{[H^+]}{K_2} + 1}$$

	Slope	Intercept
<ul style="list-style-type: none"> <li>• Lines for S<sup>-2</sup> <ul style="list-style-type: none"> <li>• Low pH (pH &lt;&lt; pK<sub>1</sub>, or [H<sup>+</sup>] &gt;&gt; K<sub>1</sub>)                             <ul style="list-style-type: none"> <li>• <math>\alpha_2 = K_1 K_2/[H^+]^2</math> or <math>[S^{2-}] = C_T K_1 K_2/[H^+]^2</math></li> <li>• <math>\log[S^{2-}] = \log C_T - pK_1 - pK_2 + 2pH</math></li> </ul> </li> <li>• Intermediate pH (pK<sub>1</sub> &lt;&lt; pH &lt;&lt; pK<sub>2</sub>, or K<sub>1</sub> &gt;&gt; [H<sup>+</sup>] &gt;&gt; K<sub>2</sub>)                             <ul style="list-style-type: none"> <li>• <math>\alpha_2 = K_2/[H^+]</math> or <math>[S^{2-}] = C_T K_2/[H^+]</math></li> <li>• <math>\log[S^{2-}] = \log C_T - pK_2 + pH</math></li> </ul> </li> <li>• High pH (pK<sub>2</sub> &lt;&lt; pH, or K<sub>2</sub> &gt;&gt; [H<sup>+</sup>])                             <ul style="list-style-type: none"> <li>• <math>\alpha_2 = 1</math> or <math>[S^{2-}] = C_T</math></li> <li>• <math>\log[S^{2-}] = \log C_T</math></li> </ul> </li> </ul> </li> </ul>	+2	-21+Log C <sub>T</sub>
	+1	-14 +log C <sub>T</sub>
	0	log C <sub>T</sub>

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## Alpha summary

	$\alpha_0$	$\alpha_1$	$\alpha_2$	$\alpha_3$
Monoprotic	$\frac{1}{1 + \frac{K_a}{[H^+]}}$	$\frac{1}{\frac{[H^+]}{K_a} + 1}$		$\sum_{i=0}^3$
Diprotic	$\frac{1}{1 + \frac{K_1}{[H^+]} + \frac{K_1 K_2}{[H^+]^2}}$	$\frac{1}{\frac{[H^+]}{K_1} + 1 + \frac{K_2}{[H^+]}}$	$\frac{1}{\frac{[H^+]^2}{K_1 K_2} + \frac{[H^+]}{K_2} + 1}$	
Triprotic	$1 + \frac{K_1}{[H^+]} + \frac{K_1 K_2}{[H^+]^2} + \frac{K_1 K_2 K_3}{[H^+]^3} = \alpha_0$			

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## In-class Practice

- $10^{-4}$  M  $\text{NaHCO}_3$
- $10^{-3}$  M  $\text{NaKHPO}_4$
- $10^{-3}$  M  $\text{H}_2\text{S}$  +  $10^{-4}$  M  $\text{NaOCl}$
- $10^{-2}$  M  $\text{H}_2\text{CO}_3$  +  $10^{-2}$  M  $\text{Na}_2\text{S}$
- $10^{-2}$  M  $\text{NaHS}$  +  $10^{-3}$  M  $\text{Na}_2\text{S}$

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NAME	EQUILIBRIA	pK <sub>a</sub>
Perchloric acid	$\text{HClO}_4 = \text{H}^+ + \text{ClO}_4^-$	-7 STRONG
Hydrochloric acid	$\text{HCl} = \text{H}^+ + \text{Cl}^-$	-3
Sulfuric acid	$\text{H}_2\text{SO}_4 = \text{H}^+ + \text{HSO}_4^-$	-3 (&2) ACIDS
Nitric acid	$\text{HNO}_3 = \text{H}^+ + \text{NO}_3^-$	-0
Hydronium ion	$\text{H}_3\text{O}^+ = \text{H}^+ + \text{H}_2\text{O}$	0
Trichloroacetic acid	$\text{CCl}_3\text{COOH} = \text{H}^+ + \text{CCl}_3\text{COO}^-$	0.70
Iodic acid	$\text{HIO}_3 = \text{H}^+ + \text{IO}_3^-$	0.8
Dichloroacetic acid	$\text{CHCl}_2\text{COOH} = \text{H}^+ + \text{CHCl}_2\text{COO}^-$	1.48
Bisulfate ion	$\text{HSO}_4^- = \text{H}^+ + \text{SO}_4^{2-}$	2
Phosphoric acid	$\text{H}_3\text{PO}_4 = \text{H}^+ + \text{H}_2\text{PO}_4^-$	2.15 (&7.2,12.3)
Ferric ion	$\text{Fe}(\text{H}_2\text{O})_6^{+3} = \text{H}^+ + \text{Fe}(\text{OH})(\text{H}_2\text{O})_5^{+2}$	2.2 (&4.6)
Chloroacetic acid	$\text{CH}_2\text{ClCOOH} = \text{H}^+ + \text{CH}_2\text{ClCOO}^-$	2.85
o-Phthalic acid	$\text{C}_6\text{H}_4(\text{COOH})_2 = \text{H}^+ + \text{C}_6\text{H}_4(\text{COOH})\text{COO}^-$	2.89 (&5.51)
Citric acid	$\text{C}_3\text{H}_5\text{O}(\text{COOH})_3 = \text{H}^+ + \text{C}_3\text{H}_5\text{O}(\text{COOH})_2\text{COO}^-$	3.14 (&4.77,6.4)
Hydrofluoric acid	$\text{HF} = \text{H}^+ + \text{F}^-$	3.2
Formic Acid	$\text{HCOOH} = \text{H}^+ + \text{HCOO}^-$	3.75
Aspartic acid	$\text{C}_2\text{H}_6\text{N}(\text{COOH})_2 = \text{H}^+ + \text{C}_2\text{H}_6\text{N}(\text{COOH})\text{COO}^-$	3.86 (&9.82)
m-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COOH} = \text{H}^+ + \text{C}_6\text{H}_4(\text{OH})\text{COO}^-$	4.06 (&9.92)
Succinic acid	$\text{C}_2\text{H}_4(\text{COOH})_2 = \text{H}^+ + \text{C}_2\text{H}_4(\text{COOH})\text{COO}^-$	4.16 (&5.61)
p-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COOH} = \text{H}^+ + \text{C}_6\text{H}_4(\text{OH})\text{COO}^-$	4.48 (&9.32)
Nitrous acid	$\text{HNO}_2 = \text{H}^+ + \text{NO}_2^-$	4.5
Ferric Monohydroxide	$\text{FeOH}(\text{H}_2\text{O})_5^{+2} + \text{H}^+ + \text{Fe}(\text{OH})_2(\text{H}_2\text{O})_4^+$	4.6
Acetic acid	$\text{CH}_3\text{COOH} = \text{H}^+ + \text{CH}_3\text{COO}^-$	4.75
Aluminum ion	$\text{Al}(\text{H}_2\text{O})_6^{+3} = \text{H}^+ + \text{Al}(\text{OH})(\text{H}_2\text{O})_5^{+2}$	4.8

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NAME	FORMULA	pK <sub>a</sub>
Propionic acid	$\text{C}_2\text{H}_5\text{COOH} = \text{H}^+ + \text{C}_2\text{H}_5\text{COO}^-$	4.87
Carbonic acid	$\text{H}_2\text{CO}_3 = \text{H}^+ + \text{HCO}_3^-$	6.35 (&10.33)
Hydrogen sulfide	$\text{H}_2\text{S} = \text{H}^+ + \text{HS}^-$	7.02 (&13.9)
Dihydrogen phosphate	$\text{H}_2\text{PO}_4^- = \text{H}^+ + \text{HPO}_4^{2-}$	7.2
Hypochlorous acid	$\text{HOCl} = \text{H}^+ + \text{OCl}^-$	7.5
Copper ion	$\text{Cu}(\text{H}_2\text{O})_6^{+2} = \text{H}^+ + \text{CuOH}(\text{H}_2\text{O})_5^+$	8.0
Zinc ion	$\text{Zn}(\text{H}_2\text{O})_6^{+2} = \text{H}^+ + \text{ZnOH}(\text{H}_2\text{O})_5^+$	8.96
Boric acid	$\text{B}(\text{OH})_3 + \text{H}_2\text{O} = \text{H}^+ + \text{B}(\text{OH})_4^-$	9.2 (&12.7,13.8)
Ammonium ion	$\text{NH}_4^+ = \text{H}^+ + \text{NH}_3$	9.24
Hydrocyanic acid	$\text{HCN} = \text{H}^+ + \text{CN}^-$	9.3
p-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COO}^- = \text{H}^+ + \text{C}_6\text{H}_4(\text{O})\text{COO}^{2-}$	9.32
Orthosilicic acid	$\text{H}_4\text{SiO}_4 = \text{H}^+ + \text{H}_3\text{SiO}_4^-$	9.86 (&13.1)
Phenol	$\text{C}_6\text{H}_5\text{OH} = \text{H}^+ + \text{C}_6\text{H}_5\text{O}^-$	9.9
m-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COO}^- = \text{H}^+ + \text{C}_6\text{H}_4(\text{O})\text{COO}^{2-}$	9.92
Cadmium ion	$\text{Cd}(\text{H}_2\text{O})_6^{+2} = \text{H}^+ + \text{CdOH}(\text{H}_2\text{O})_5^+$	10.2
Bicarbonate ion	$\text{HCO}_3^- = \text{H}^+ + \text{CO}_3^{2-}$	10.33
Magnesium ion	$\text{Mg}(\text{H}_2\text{O})_6^{+2} = \text{H}^+ + \text{MgOH}(\text{H}_2\text{O})_5^+$	11.4
Monohydrogen phosphate	$\text{HPO}_4^{2-} = \text{H}^+ + \text{PO}_4^{3-}$	12.3
Calcium ion	$\text{Ca}(\text{H}_2\text{O})_6^{+2} = \text{H}^+ + \text{CaOH}(\text{H}_2\text{O})_5^+$	12.5
Trihydrogen silicate	$\text{H}_3\text{SiO}_4^- = \text{H}^+ + \text{H}_2\text{SiO}_4^{2-}$	12.6
Bisulfide ion	$\text{HS}^- = \text{H}^+ + \text{S}^{2-}$	13.9
Water	$\text{H}_2\text{O} = \text{H}^+ + \text{OH}^-$	14.00
Ammonia	$\text{NH}_3 = \text{H}^+ + \text{NH}_2^-$	23
Hydroxide	$\text{OH}^- = \text{H}^+ + \text{O}^{2-}$	24
Methane	$\text{CH}_4 = \text{H}^+ + \text{CH}_3^-$	34

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## Multiple acids

- Solve problems in class
- Two different acids?
  - e.g.,  $10^{-5}$  HF and  $10^{-4}$   $\text{NH}_4\text{Cl}$
  - e.g.,  $10^{-3}$  acetic acid and  $10^{-2}$  hypochlorous
- Acid and conjugate base pair?
  - e.g., carbonic acid and bicarbonate
  - e.g.,  $9 \times 10^{-3}$   $\text{HNO}_2$  +  $10^{-3}$   $\text{NaNO}_2$
  - don't try to use the PBE, it won't work very well. Use the ENE (CBE) instead

- To next lecture

DAR