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# CEE 680: Water Chemistry

## Lecture #6

Acids & Bases: Analytical Solutions  
(Stumm & Morgan, Chapt.3 )

(Benjamin, Chapt. 3; pg.131-150)

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## Definitions

- Early
- Acids
  - turns blue litmus red
  - tastes sour
  - neutralizes bases
  - reacts with active metals to evolve H<sub>2</sub>
- Bases
  - turns red litmus blue
  - tastes bitter
  - feels soapy

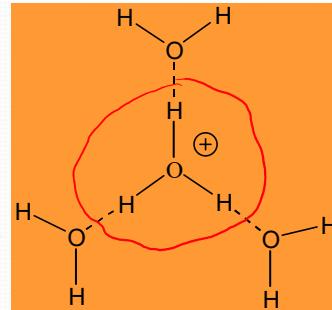
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## Definitions (cont.)

- Arrhenius (1887)

- Acids

- solutions which contain an excess of hydrogen ions
    - e.g.,  $\text{HNO}_3 = \text{H}^+ + \text{NO}_3^-$
    - $\text{H}^+$  doesn't exist free in solution



- Bases

- solutions which contain an excess of hydroxide ions

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## Definitions (cont.)

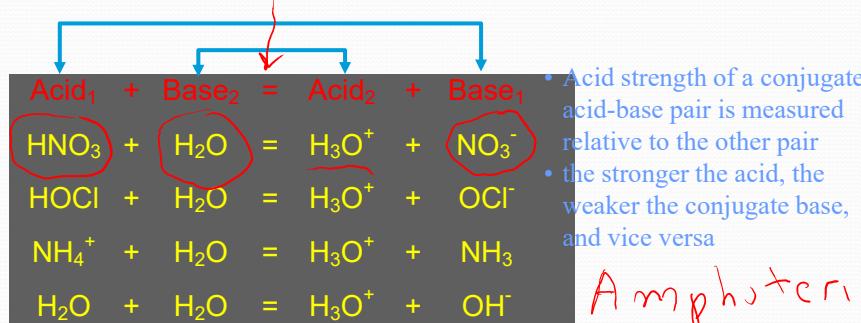
- Bronsted-Lowry (1923)

- Acids: (proton donor)

- any substance that can donate a proton to any other substance

- Bases: (proton acceptor)

- any substance that accepts a proton from any other substance



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## Definitions (cont.)

- Lewis
  - Acids
    - can accept and share a lone pair of electrons
  - Bases
    - can donate and share a lone pair of electrons

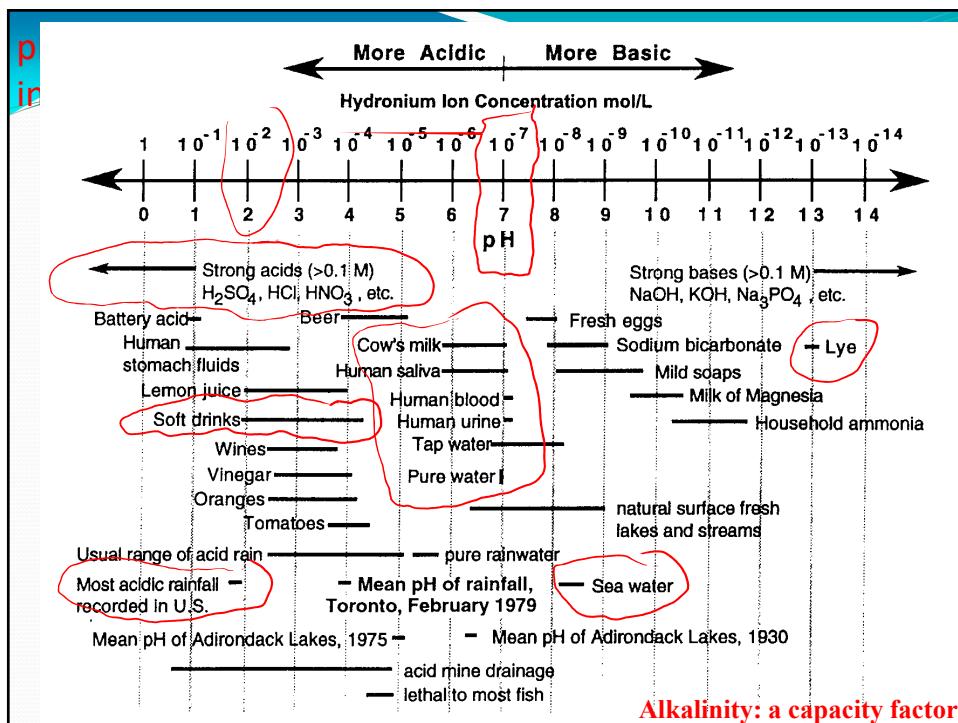
$$K_w = 10^{-14} = [H^+][OH^-]$$

A more general definition:  
includes metal ions as acids

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## What are the limits of pH?

- How low can you go?
  - Volcanic lakes
    - Lake Katanuma in Japan; pH = 1.7
  - Hot springs
    - Near Ebeko Volcano in Russia; pH = -1.7
  - Acid mine drainage
    - Richmond mine near Redding CA, pH = -3.6

Nordstrom et al., 2000  
[ES&T 34:254]

From: Brezonik & Arnold, 2011

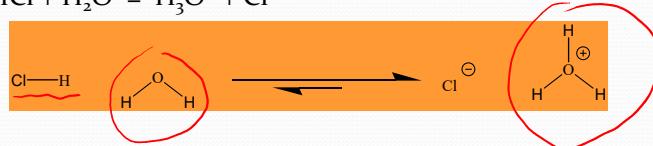
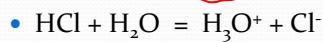
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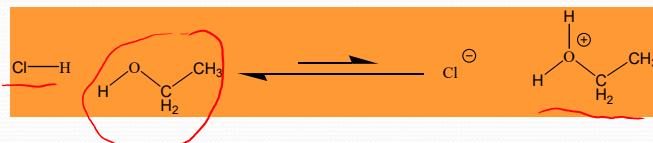
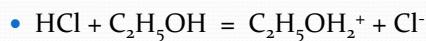
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## Effect of proton acceptor

- Strong acid in water



- Weak acid in organic solvent (ethanol)



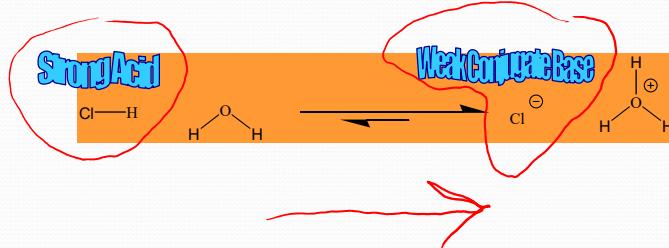
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## Acid/Conjugate Base

- Weak acids do not substantially donate a proton
  - e.g.,  $\text{H}_2\text{CO}_3$ ,  $\text{HAc}$ ,  $\text{H}_2\text{S}$ ,  $\text{HOCl}$
- The stronger an acid is the weaker its conjugate base.  
The stronger a base is the weaker its conjugate acid



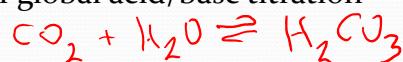
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## Acids & Bases

- pH of most mineral-bearing waters is 6 to 9. (fairly constant)
- pH and composition of natural waters is regulated by reactions of acids & bases
  - chemical reactions; mostly with minerals
    - carbonate rocks: react with  $\text{CO}_2$  (an acid)
      - $\text{CaCO}_3 + \text{CO}_2 = \text{Ca}^{+2} + 2\text{HCO}_3^-$
    - other bases are also formed:  $\text{NH}_3$ , silicates, borate, phosphate
    - acids from volcanic activity:  $\text{HCl}$ ,  $\text{SO}_2$
  - Biological reactions: photosynthesis & resp.
  - Sillen: Ocean is result of global acid/base titration



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## Acids & Bases (cont.)

- Equilibrium is rapidly established
  - proton transfer is very fast
- we call  $[H^+]$  the **Master Variable**
  - because Protons react with so many chemical species, affect equilibria and rates
- Strength of acids & bases
  - strong acids have a substantial tendency to donate a proton. This depends on the nature of the acid as well as the base accepting the proton (often water).

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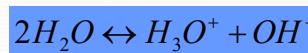
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### Autodissociation of water



- Actually donation of proton to neighboring water



$$K_w = \frac{\{H^+\}\{OH^-\}}{\{H_2O\}}$$

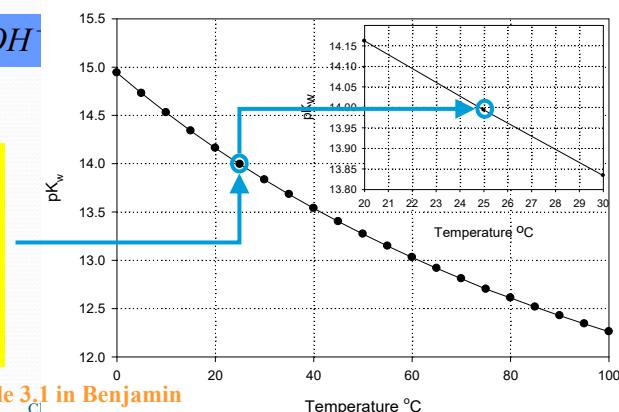
✓ ✓

$$\approx \{H^+\}\{OH^-\}$$

$$\approx 10^{-14} @ 25^\circ C$$

See Table 3.1 in Benjamin

Cl



## Mathematical Expression of Acid/Base Strength

- Equilibrium constant
  - acids:  $\text{HA} = \text{H}^+ + \text{A}^-$
  - $\text{HCl} + \text{H}_2\text{O} = \text{H}_3\text{O}^+ + \text{Cl}^-$
  - $\text{HCl} = \text{H}^+ + \text{Cl}^-$
- Bases:  $\text{B} + \text{H}_2\text{O} = \text{BH}^+ + \text{OH}^-$
- $\text{NH}_3 + \text{H}_2\text{O} = \text{NH}_4^+ + \text{OH}^-$

$$K_a = \frac{[\text{H}^+][\text{Cl}^-]}{[\text{HCl}]} \approx 10^3$$

$\text{pH} = 7$     $\text{pH} = 0$

$$\frac{[\text{Cl}^-]}{[\text{HCl}]} = ? \quad 10^{10}$$

$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} = 10^{-4.76}$$

10<sup>3</sup>

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## Relationship between $K_a$ and $K_b$

- For the  $\text{NH}_3/\text{NH}_4^+$  pair
  - $\text{NH}_4^+ = \text{NH}_3 + \text{H}^+$
  - $\text{NH}_3 + \text{H}_2\text{O} = \text{NH}_4^+ + \text{OH}^-$
- combining

$$K_a = \frac{[\text{H}^+][\text{NH}_3]}{[\text{NH}_4^+]} = 10^{-9.24}$$

$$K_b = \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} = 10^{-4.76}$$

$$\rightarrow K_a K_b = \left( \frac{[\text{H}^+][\text{NH}_3]}{[\text{NH}_4^+]} \right) \left( \frac{[\text{NH}_4^+][\text{OH}^-]}{[\text{NH}_3]} \right) = 10^{-9.24} 10^{-4.76}$$

$$K_a K_b = [\text{H}^+][\text{OH}^-] = 10^{-14.00} = K_w$$

See Table 3.1 (pg.94) for values of  $K_w$  at various pHs

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NAME	EQUILIBRIA	pKa
Perchloric acid	$\text{HClO}_4 = \text{H}^+ + \text{ClO}_4^-$	-7 STRONG
Hydrochloric acid	$\text{HCl} = \text{H}^+ + \text{Cl}^-$	-3
Sulfuric acid	$\text{H}_2\text{SO}_4 = \text{H}^+ + \text{HSO}_4^-$	-3 (&2) ACIDS
Nitric acid	$\text{HNO}_3 = \text{H}^+ + \text{NO}_3^-$	-0
Hydronium ion	$\text{H}_3\text{O}^+ = \text{H}^+ + \text{H}_2\text{O}$	0
Trichloroacetic acid	$\text{CCl}_3\text{COOH} = \text{H}^+ + \text{CCl}_3\text{COO}^-$	0.70
Iodic acid	$\text{HIO}_3 = \text{H}^+ + \text{IO}_3^-$	0.8
Dichloroacetic acid	$\text{CHCl}_2\text{COOH} = \text{H}^+ + \text{CHCl}_2\text{COO}^-$	1.48
Bisulfate ion	$\text{HSO}_4^- = \text{H}^+ + \text{SO}_4^{2-}$	2
Phosphoric acid	$\text{H}_3\text{PO}_4 = \text{H}^+ + \text{H}_2\text{PO}_4^-$	2.15 (&7.2, 12.3)
Ferric ion	$\text{Fe}(\text{H}_2\text{O})_6^{3-} = \text{H}^+ + \text{Fe}(\text{OH})(\text{H}_2\text{O})_5^+$	2.2 (&4.6)
Chloroacetic acid	$\text{CH}_2\text{ClCOOH} = \text{H}^+ + \text{CH}_2\text{ClCOO}^-$	2.85
o-Phthalic acid	$\text{C}_6\text{H}_4(\text{COOH})_2 = \text{H}^+ + \text{C}_6\text{H}_4(\text{COOH})\text{COO}^-$	2.89 (&5.51)
Citric acid	$\text{C}_3\text{H}_5\text{O}(\text{COOH})_3 = \text{H}^+ + \text{C}_3\text{H}_5\text{O}(\text{COOH})_2\text{COO}^-$	3.14 (&4.77, 6.4)
Hydrofluoric acid	$\text{HF} = \text{H}^+ + \text{F}^-$	3.2
Formic Acid	$\text{HCOOH} = \text{H}^+ + \text{HCOO}^-$	3.75
Aspartic acid	$\text{C}_2\text{H}_6\text{N}(\text{COOH})_2 = \text{H}^+ + \text{C}_2\text{H}_6\text{N}(\text{COOH})\text{COO}^-$	3.86 (&9.82)
m-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COOH} = \text{H}^+ + \text{C}_6\text{H}_4(\text{OH})\text{COO}^-$	4.06 (&9.92)
Succinic acid	$\text{C}_2\text{H}_4(\text{COOH})_2 = \text{H}^+ + \text{C}_2\text{H}_4(\text{COOH})\text{COO}^-$	4.16 (&5.61)
p-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COOH} = \text{H}^+ + \text{C}_6\text{H}_4(\text{OH})\text{COO}^-$	4.48 (&9.32)
Nitrous acid	$\text{HNO}_2 = \text{H}^+ + \text{NO}_2^-$	4.5
Ferric Monohydroxide	$\text{Fe}(\text{OH})(\text{H}_2\text{O})_5^{2+} + \text{H}^+ + \text{Fe}(\text{OH})_2(\text{H}_2\text{O})_4^+$	4.6
Acetic acid	$\text{CH}_3\text{COOH} = \text{H}^+ + \text{CH}_3\text{COO}^-$	4.75
Aluminum ion	$\text{Al}(\text{H}_2\text{O})_6^{3-} = \text{H}^+ + \text{Al}(\text{OH})(\text{H}_2\text{O})_5^+$	4.8

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NAME	FORMULA	pKa
Propionic acid	$\text{C}_2\text{H}_5\text{COOH} = \text{H}^+ + \text{C}_2\text{H}_5\text{COO}^-$	4.87
Carbonic acid	$\text{H}_2\text{CO}_3 = \text{H}^+ + \text{HCO}_3^-$	6.35 (&10.33)
Hydrogen sulfide	$\text{H}_2\text{S} = \text{H}^+ + \text{HS}^-$	7.02 (&13.9)
Dihydrogen phosphate	$\text{H}_2\text{PO}_4^- \rightleftharpoons \text{H}^+ + \text{HPO}_4^{2-}$	7.2
Hypochlorous acid	$\text{HOCl} = \text{H}^+ + \text{OCl}^-$	7.5
Copper ion	$\text{Cu}(\text{H}_2\text{O})_6^{2+} = \text{H}^+ + \text{CuOH}(\text{H}_2\text{O})_5^+$	8.0
Zinc ion	$\text{Zn}(\text{H}_2\text{O})_6^{2+} = \text{H}^+ + \text{ZnOH}(\text{H}_2\text{O})_5^+$	8.96
Boric acid	$\text{B}(\text{OH})_3 + \text{H}_2\text{O} = \text{H}^+ + \text{B}(\text{OH})_4^-$	9.2 (&12.7, 13.8)
Ammonium ion	$\text{NH}_4^+ = \text{H}^+ + \text{NH}_3$	9.24
Hydrocyanic acid	$\text{HCN} = \text{H}^+ + \text{CN}^-$	9.3
p-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COO}^- = \text{H}^+ + \text{C}_6\text{H}_4(\text{O})\text{COO}^-$	9.32
Orthosilicic acid	$\text{H}_4\text{SiO}_4 = \text{H}^+ + \text{H}_3\text{SiO}_4^-$	9.86 (&13.1)
Phenol	$\text{C}_6\text{H}_5\text{OH} = \text{H}^+ + \text{C}_6\text{H}_5\text{O}^-$	9.9
m-Hydroxybenzoic acid	$\text{C}_6\text{H}_4(\text{OH})\text{COO}^- = \text{H}^+ + \text{C}_6\text{H}_4(\text{O})\text{COO}^-$	9.92
Cadmium ion	$\text{Cd}(\text{H}_2\text{O})_6^{2+} = \text{H}^+ + \text{CdOH}(\text{H}_2\text{O})_5^+$	10.2
Bicarbonate ion	$\text{HCO}_3^- = \text{H}^+ + \text{CO}_3^{2-}$	10.33
Magnesium ion	$\text{Mg}(\text{H}_2\text{O})_6^{2+} = \text{H}^+ + \text{MgOH}(\text{H}_2\text{O})_5^+$	11.4
Monohydrogen phosphate	$\text{HPO}_4^{2-} \rightleftharpoons \text{H}^+ + \text{PO}_4^{3-}$	12.3
Calcium ion	$\text{Ca}(\text{H}_2\text{O})_6^{2+} = \text{H}^+ + \text{CaOH}(\text{H}_2\text{O})_5^+$	12.5
Trihydrogen silicate	$\text{H}_3\text{SiO}_4^- = \text{H}^+ + \text{H}_2\text{SiO}_4^{2-}$	12.6
Bisulfide ion	$\text{HS}^- = \text{H}^+ + \text{S}^{2-}$	13.9
Water	$\text{H}_2\text{O} = \text{H}^+ + \text{OH}^-$	14.00
Ammonia	$\text{NH}_3 = \text{H}^+ + \text{NH}_2^-$	23
Hydroxide	$\text{OH}^- = \text{H}^+ + \text{O}^{2-}$	24
Methane	$\text{CH}_4 = \text{H}^+ + \text{CH}_3^-$	34

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## Analytical Solutions

- Basic Approach

- combine mass balances with thermodynamic equilibria
- consider exact solutions, as well as approximations
- similar approaches used for other topics in CEE 680

- Four principal steps

- 1. List all species present
- 2. List all independent equations
  - equilibria, mass balances, proton balance (or electroneutrality equation)
- 3. Combine equations and solve for proton
- 4. Solve for other species

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## General Example

- 1. List all species present

- $H^+$ ,  $OH^-$ ,  $HA$ ,  $A^-$

Four total

- 2. List all independent equations

- equilibria

- $K_a = [H^+][A^-]/[HA]$

①

- $K_w = [H^+][OH^-]$

②

- mass balances

- $[HA] + [A^-] = C$  (formal or “analytical” concentration)

③

- proton balance (or electroneutrality equation)

- $PBE: \sum(\text{proton rich species}) = \sum(\text{proton poor species})$

- $ENE: \sum(\text{cationic species}) = \sum(\text{anionic species})$

- $[H^+] = [OH^-] + [A^-]$

④

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## General Example (cont.)

- 3. Combine equations and solve for proton
  - use PBE or ENE and eliminate non-H<sup>+</sup> species by substituting in the other equations
- 4. Solve for other species

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## Acetic Acid Example

- What is the pH and solution composition when you add 1 mM acetic acid to 1 liter of water

- The Reaction:



- The overall Gibbs Free Energy:

$$\Delta G^\circ = \sum v_i \Delta G_f^\circ$$

- Recall:

$$\Delta G_f^\circ_{f-Ac^-} + \Delta G_f^\circ_{f-H^+} - \Delta G_f^\circ_{f-HAc}$$

$$= -88.29 - 0 - (-94.8) = +6.51 \text{ Kcal}$$

- at 25°C:

$$\Delta G^\circ = -RT \ln K$$

$$= -2.303RT \log K$$

- so for this problem:

$$\Delta G^\circ = -2.303(0.001987)(298.13) \log K$$

$$= -1.364 \log K$$

$$\log K = -\frac{\Delta G^\circ}{1.364} = -\frac{6.51}{1.364} = -4.77$$

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## Acetic Acid Example (cont.)

- 1. List all species present
  - $\text{H}^+$ ,  $\text{OH}^-$ ,  $\text{HAc}$ ,  $\text{Ac}^-$  **Four total**
- 2. List all independent equations
  - equilibria
    - $K_a = [\text{H}^+][\text{Ac}^-]/[\text{HAc}] = 10^{-4.77}$  **①**
    - $K_w = [\text{H}^+][\text{OH}^-] = 10^{-14}$  **②**
  - mass balances
    - $C = [\text{HAc}] + [\text{Ac}^-] = 10^{-3}$  **③**
  - proton balance:  $\Sigma(\text{proton rich species}) = \Sigma(\text{proton poor species})$ 
    - $\text{HAc} \xrightarrow{\text{H}_2\text{O}} [\text{H}^+] = [\text{OH}^-] + [\text{Ac}^-]$  **④**

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## HAc Example (cont.)

- 3. Combine equations and solve for  $\text{H}^+$ 
  - **④**  $[\text{H}^+] = [\text{OH}^-] + [\text{Ac}^-]$
  - **②**  $[\text{OH}^-] = K_w/[\text{H}^+]$
  - **②+④**  $[\text{H}^+] = K_w/[\text{H}^+] + [\text{Ac}^-]$
  - **②+③+④**  $[\text{H}^+] = K_w/[\text{H}^+] + K_a C/[K_a + [\text{H}^+]]$ 
    - $[\text{H}^+]^2 = K_w + K_a C[\text{H}^+]/[K_a + [\text{H}^+]]$  **③**
    - $K_a [\text{H}^+]^2 + [\text{H}^+]^3 = K_w K_a + K_w [\text{H}^+] + K_a C [\text{H}^+]$
    - $[\text{H}^+]^3 + K_a [\text{H}^+]^2 - \{K_w + K_a C\} [\text{H}^+] - K_w K_a = 0$
- 4. Solve for other species
  - **①**  $K_a = [\text{H}^+][\text{Ac}^-]/[\text{HAc}]$
  - **①+③**  $K_a = [\text{H}^+][\text{Ac}^-]/\{C - [\text{Ac}^-]\}$
  - $K_a C - K_a [\text{Ac}^-] = [\text{H}^+][\text{Ac}^-]$
  - $K_a C = [\text{Ac}^-]\{K_a + [\text{H}^+\}]$
  - $[\text{Ac}^-] = K_a C / \{K_a + [\text{H}^+\}\}$

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## Exact Solution

- Exact solution:  $\text{pH} = 3.913$

- $[\text{H}^+] = 1.22 \times 10^{-4}$

$$[\text{OH}^-] = K_w / [\text{H}^+]$$

- $[\text{OH}^-] = 8.19 \times 10^{-11}$

$$[\text{Ac}^-] = K_a C / \{K_a + [\text{H}^+]\}$$

- $[\text{Ac}^-] = 1.22 \times 10^{-4}$

$$[\text{HAc}] = C - [\text{Ac}^-]$$

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- To next lecture

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