

Updated: 16 April 2013 [Print version](#)

CEE 577: Surface Water Quality Modeling

Lecture #29
Toxics: Lake Models, Sorption
 QUAL2E: tutorial
 (Chapra, L40 & L41)

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Steady State Solution

- Water column

$$C_1 = \frac{Qc_{in}}{Q + k_1V_1 + v_v Af_{d1} + (1 - F'_r)(v_s f_{p1} + v_d f_{d1})A}$$

- Mixed Sediments

$$C_2 = \frac{v_s f_{p1} + v_d f_{d1}}{k_2 H_2 + v_r + v_b + v_d f_{d2}} C_1$$

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Sediment Feedback & k

- The ratio of sediment feedback to total sediment purging

$$F'_r = \frac{v_r + v_d f_{d2}}{v_r + v_b + v_d f_{d2} + k_2 H_2}$$

- The first-order constants k_1 and k_2 incorporate various decay processes
 - Biodegradation
 - Hydrolysis
 - photolysis

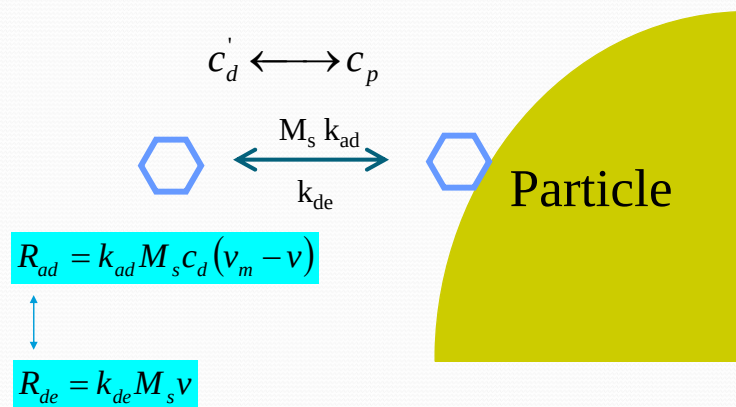
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Sorption

- Langmuir Isotherm



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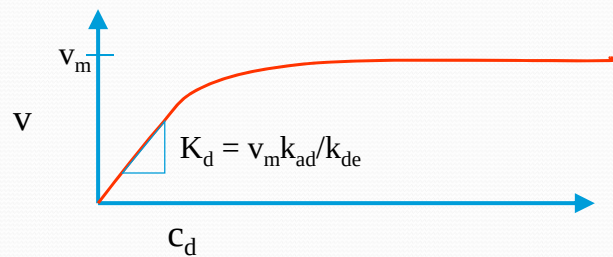
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Langmuir Isotherm

- At equilibrium, $R_{ad}=R_{de}$

$$v = \frac{v_m C_d}{\left(\frac{k_{de}}{k_{ad}} \right) + C_d}$$

- Which gives the Langmuir Isotherm



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Linear Partitioning

$$v = K_d C_d$$

- When appropriate
 - Predicted at low C_d 's with Langmuir isotherm
 - Expected for all C_d 's when solute is thought undergo ideal "dissolution" in organic layers
- Significance
 - particulate phase concentration is obtained from dissolved by

$$C_p = mv = mK_d C_d$$

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Development of fractions

- Recapitulating and combining, we get:

$$\begin{aligned} c_p &= mv \\ &= mK_d c_d \end{aligned}$$

$$\begin{aligned} c &= c_d + c_p \\ &= c_d + mK_d c_d \end{aligned}$$

- and the fractions can be expressed as:

$$\begin{aligned} f_d &\equiv \frac{c_d}{c} = \frac{c_d}{c_d + mK_d c_d} \\ &= \frac{1}{1 + K_d m} \end{aligned}$$

$$\begin{aligned} f_p &\equiv \frac{c_p}{c} = \frac{mK_d c_d}{c_d + mK_d c_d} \\ &= \frac{K_d m}{1 + K_d m} \end{aligned}$$

- To next lecture