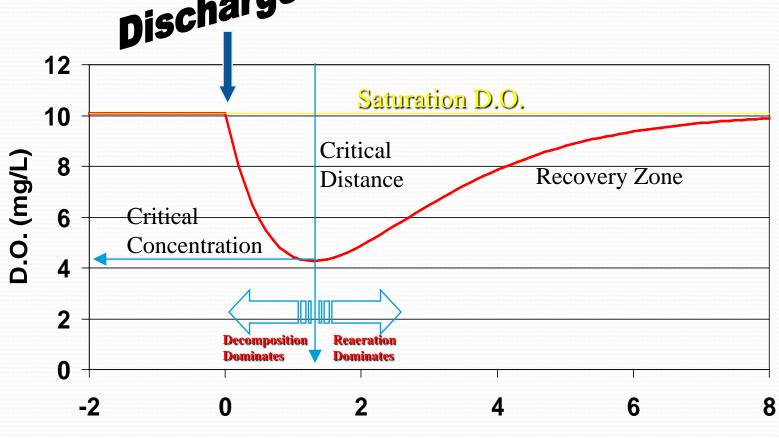
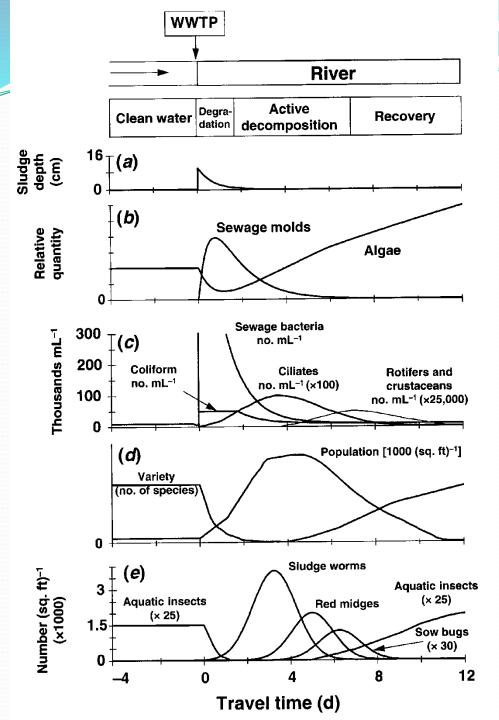
CEE 577: Surface Water Quality Modeling

Lecture #14
Gas Transfer & Reaeration
(Chapra, L20 & L21)

Typical DO Sag Curve pischarge



Distance Downstream (miles)



Effect of WWTP Effluent on Stream Biota

• From Chapra, Figure 19.3 (pg.350)

Gas Transfer: Equilibria

Henry's Law

$$C_A = K_H p_A$$

where,

C_A = concentration of species A at equilibrium, [mol/L or mg/L]

K_H = Henry's Law constant for species A, [mol/L-atm or mg/L-atm]

 p_A = partial pressure gas A exerts on the liquid, [atm]

Gas Transfer: kinetics

 For a typical water system, the change in concentration of the gas with time can be expressed as:

where,
$$\frac{dC}{dt} = -k_L a(C_s - C_t)$$

$$k_L a = \text{gas transfer coefficient, [time}^{-1}]$$

 $C_t = concentration at time t, [mol/L or mg/L]$ $C_s = saturation concentration from Henry's Law.$

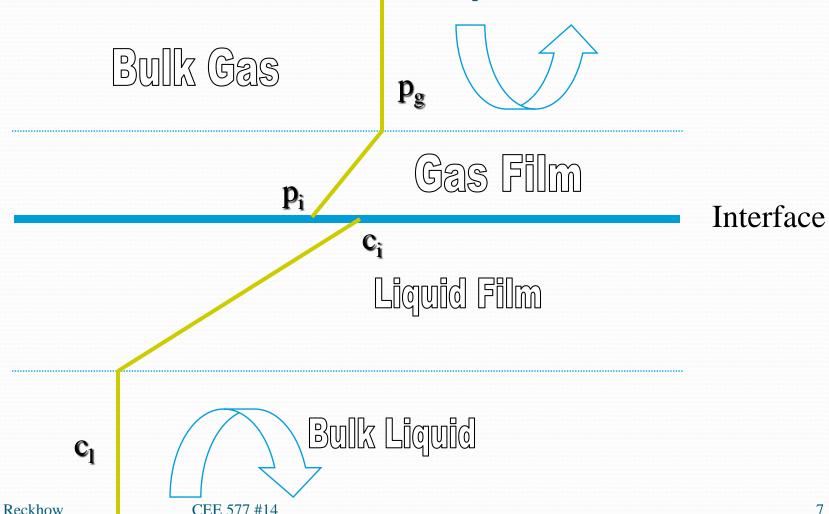
 k_La is actually the gas transfer coefficient k_L times the specific surface area, a, where a is the bubble surface area divided by the bubble volume. It is quite difficult to determine the two parameters separately. Since they are normally used together a separate determination is not necessary.

Analyzing Gas Transfer Data

The above equation can be separated and integrated from $C = C_0$ at t = 0 to $C = C_t$ at t = t, yielding:

$$\ln \frac{\left(C_{s} - C_{t}\right)}{\left(C_{s} - C_{o}\right)} = -k_{L}at$$

The two film theory



David Reckhow

• To next lecture